



# Elastic moduli of $\text{XAlSiO}_4$ aluminosilicate glasses: effects of charge-balancing cations



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## ARTICLE INFO

### Article history:

Received 2 May 2016

Received in revised form 10 June 2016

Accepted 15 June 2016

Available online xxxx

### Keywords:

Aluminosilicate glasses

Tectosilicate

Elastic properties

Density

Glass transition temperature

Brillouin scattering

## ABSTRACT

Brillouin spectroscopy is used to investigate the elastic properties of  $\text{XAlSiO}_4$  aluminosilicate glasses where  $\text{X} = \text{Li}, \text{Na}, \text{K}, \text{Mg}_{0.5}, \text{Ca}_{0.5}, \text{Sr}_{0.5}, \text{Ba}_{0.5}, \text{and Zn}_{0.5}$ . The Brillouin frequency shifts obtained in two different scattering geometries allow the calculation of the refractive index, the two sound velocities and Poisson's ratio. Measurements of the mass density give in turn the elastic moduli and the Debye temperature. We find that the elastic properties scale with the atomic density of the glassy network or the charge-balancing cation field strength while they negatively correlate with the glass transition temperature. Further, Poisson's ratio depends on the nature of the non-framework cations in this glass series.

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## 1. Introduction

About 85% of the atoms in the Earth's crust are oxygen and silicon atoms forming a myriad of silicate compounds when combined with alkali, alkaline earth or other metals. Aluminum being the most abundant metal in the crust, the crucial role of aluminosilicates in earth sciences is manifest. High-value aluminosilicate glasses and glass-ceramics are widely used in currently emerging technologies due to their attractive mechanical, optical or refractory properties [1,2].

Elasticity is a fundamental property of materials and as such is used in the determination of various physical properties in glass science, such as thermal shock resistance, thermal optical coefficients or fracture toughness. Indeed, the elastic modulus gives a global view of a material stiffness and reflects both the network connectivity and the inter-atomic potentials. It is then quite surprising to observe that the elastic properties of some simple glass compositions, e.g. ternary aluminosilicate glasses, are not known yet. It probably relies on the difficulty of bypassing the crystallization for some compositions, and further, on obtaining sufficiently large bubble-free samples to carry on ultrasonic experiments.

In the present paper, we investigate physical properties of a series of charge-compensated aluminosilicate glasses comprising 50% mol  $\text{SiO}_2$ .

The total concentration of charge compensator oxides being equal to that of alumina, the glass structure is expected to be an almost fully connected, three-dimensional, random aluminosilicate network of tetrahedral units in which the charge compensation for the negatively charged  $(\text{AlO}_4)^-$  tetrahedra would be provided by the  $\text{X}_{2/n}^{n+}$  cations [3–5]. Actually, these simple stoichiometric considerations must be revised since five-fold coordinated aluminum species have been shown to exist in such tectosilicate glasses [6–13], their content being related to the X cation field strength [11,13] as well as to the  $\text{SiO}_2$  content [10,11]. High temperature data also suggest that five-fold Al concentration increases with increasing temperature in tectosilicate melts [14]. We measured density, glass transition temperature, refractive index and sound velocities from which we calculated molar volume, elastic moduli and Debye temperature. The variation of the measured physical properties in these glasses, which should reflect the influence of the charge compensator cations only, is discussed.

## 2. Experimental methods

### 2.1. Glass synthesis

The eight charge-balanced  $(\text{X}_{2/n}^{n+}\text{O}^{2-}/\text{Al}_2\text{O}_3 = 1)$  aluminosilicate glasses were prepared by melting the appropriate quantities of high-purity oxide and carbonate powders according to the following protocol [15]. About 100 g of batch materials (Rectapur, Merck) was mixed and

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brunched for 60 min in alcohol using an agate mortar. The mixture was slowly heated for 24 and 72 h for alkaline earth- and alkali-bearing compositions, respectively, to decompose the carbonate, and then, heated up to 1900 K in a covered platinum crucible for a few hours in equilibrium with air. The melt was quenched in few seconds by dipping the bottom of the platinum crucible into distilled water, leading to an estimated quenching rate of  $\approx 15$  K/mn [11] across the glass transition region. This process was repeated four times to warrant the best glass homogeneity.

Glasses containing SrO and BaO oxides are hardly obtained by the above standard quenching technique due to the high liquidus temperature. Ceramic materials were then first synthesized using five melting and crunching steps [16,10]. Small amounts of materials were finally melted using an aerodynamic levitation device in air located at the CEMHTI-CNRS, Orléans, France and a CO<sub>2</sub> laser as the heating source [17]. The melting time was about 1 min. A high quenching rate of  $\approx 300$  K/mn [11] was obtained by simply switching off the power source. Clear glass beads with 1–5 mm in diameter were obtained.

All the glasses investigated here were annealed for at least 12 h at about 50–100 K below the estimated  $T_g$ . Chemical homogeneity was checked by microprobe analysis and Raman spectroscopy. The samples are labeled XA50.25 according to the charge balancing oxide  $X_{2/m}^{n+} O^{2-}$  and to the composition comprising 50% mol SiO<sub>2</sub> and 25% mol Al<sub>2</sub>O<sub>3</sub>. Mass densities  $\rho$  were measured with the Archimedes' method in toluene from which we deduced molar volumes  $V_m$ . Glass transition temperatures  $T_g$  were determined from viscosity measurements. By definition,  $T_g$  corresponds to the temperature at which the viscosity is equal to  $10^{12}$  Pa.s. Viscosity measurements were performed using a creep apparatus as detailed in [15,18,19].

## 2.2. Brillouin scattering

Brillouin scattering experiments were performed using a standard triple-pass tandem interferometer of the Vernier type designed by JRS Scientific Instruments [20]. A single line diode-pumped solid-state laser operating at  $\lambda_0 = 532.03$  nm was used to excite the samples with a power of 150 mW at the sample surface. A single photon counting avalanche photo-diode was used to record the Brillouin spectra which were taken at room temperature in both backscattering and symmetric platelet scattering geometry [21] without any polarization analysis. The backscattered light was collected by a high numerical aperture aspheric lens (NA = 0.38). In the platelet geometry, the scattered light was collected at  $\theta = 50^\circ$  to the incident laser beam by the same aspheric lens. However, the aperture was limited to a curved slit according to the spurious geometrical broadening of the Brillouin lines to the resolution of the spectrometer [22]. All the measurements were performed on samples that were optically polished on two opposite parallel faces.

For isotropic materials in backscattering geometry, sound velocities  $v$  are related to the measured Brillouin frequency shifts  $\nu_B$  by the following equation:

$$v = \frac{\nu_B \lambda_0}{2n}, \quad (1)$$

where  $\lambda_0$  is the incident laser wavelength in air and  $n$  is the refractive index of the sample at  $\lambda_0$ . The measured Brillouin lineshapes were analyzed taking into account the slight downshift of the frequency line arising from the finite aperture [23]. In the symmetric platelet geometry, the Brillouin equation reads:

$$v = \frac{\nu_B \lambda_0}{2 \sin(\theta/2)}. \quad (2)$$

Selection rules governing Brillouin scattering in isotropic materials show that longitudinal modes only are visible in perfect backscattering geometry whereas both transverse and longitudinal modes can be

measured in the symmetric platelet configuration. With combining measurements in both geometries, it is possible to obtain the two sound velocities  $v_L$ ,  $v_T$  and the refractive index of the sample at  $\lambda_0$ . The value of  $\theta$  was obtained using the Brillouin scattering from the longitudinal mode of a high purity silica glass sample (Suprasil F300, <1 ppm OH) in both geometries (Eq. (1) and (2)) and its known refractive index  $n = 1.4607$  at 532 nm. We found  $\theta = 49.80^\circ \pm 0.16^\circ$ .

## 3. Results

### 3.1. Thermo-physical properties

Table 1 summarizes the measured values of the glass transition temperature  $T_g$  and the mass density  $\rho$ , as well as the calculated molar volume  $V_m$  of the eight tectosilicate glasses. Alkali containing glasses share an almost constant  $\rho$  value with a variation of about 1% around  $2.46 \text{ g.cm}^{-3}$  whereas the mass density of the alkaline earth glasses increases significantly with the increasing molar weight of the charge compensator oxide, from about  $2.68$  to  $3.30 \text{ g.cm}^{-3}$ . Conversely, the atomic density which is inversely proportional to  $V_m$  decreases with increasing charge compensator cation size for both the alkali and the alkaline earth glasses. As shown in Fig. 1,  $V_m$  decreases non-linearly for increasing cation field strength. The latter is here defined as the ratio of the formal charge  $z$  divided by the square of the effective cation radius  $r$  [32]. Coordination numbers C.N. and corresponding effective radii  $r$  [24] used to calculate the cations field strengths  $z/r^2$  are reported in Table 1 for the eight charge-balancing cations.  $z/r^2$  increases along the series  $K^+ < Na^+ < Li^+$  and  $Ba^{2+} < Sr^{2+} < Ca^{2+} < Mg^{2+}$ . Accordingly, the cation field strength of the small transition metal cation  $Zn^{2+}$  is close to the one of  $Mg^{2+}$ . This trend in  $V_m$  probably reflects a tighter binding of oxygens to the lighter charge compensator cations, as expected from their larger field strength.

Fig. 2 displays the glass transition temperature as a function of the cation field strength.  $T_g$  decreases with  $z/r^2$ , both for alkali and alkaline earth glasses, but with very different slopes. For alkali-bearing or alkaline earth-bearing glasses,  $T_g$  is thus strongly influenced by the radius of the charge compensator cation. These trends are mostly in line with the viscosity of silica-rich XAlSi<sub>3</sub>O<sub>8</sub> melts close to  $T_g$  which increases in the order  $Li < Na < Ca < Mg < K$  [33]. We note however that for the XAlSiO<sub>4</sub> glasses here investigated, the  $T_g$  of the Ca-bearing glass is higher than the  $T_g$  of the Mg compound, in agreement with the smaller radius of the later cation. Such remarkable variations of  $T_g$  reveal a strong coupling between the aluminosilicate backbone and the non-framework cation introduced to charge-balance Al in tetrahedral coordination. It has indeed been shown that increasing the field strength of charge compensator cations leads to increasing perturbations and weakening of the aluminosilicate framework [34]. While the trends observed independently for the alkali- or alkaline earth-bearing glasses follow this simple scenario, the substitution of alkaline earth for alkali cations cannot be reconciled with it. The  $T_g$  variations could also result from modifications of the aluminosilicate network topology and/or differences in (Si, Al) distributions between alkali- and alkaline earth-bearing glasses [33,35].

### 3.2. Elastic properties

Fig. 3 shows the Brillouin scattering spectrum from the calcium-bearing aluminosilicate glass obtained in the platelet scattering geometry. For all glasses, both transverse acoustic (TA) and longitudinal acoustic (LA) Brillouin doublets were clearly observed with significant variations of their relative scattered intensities. The intense central unshifted peak is the Rayleigh line, whereas the outer pair of peaks arises from the Rayleigh ghosts of the first order transmitted by the tandem interferometer.

Poisson's ratio  $\nu$  can be readily obtained from the measured Brillouin frequency shifts of the longitudinal  $\nu_{B_L}$  and the transverse  $\nu_{B_T}$  modes in

**Table 1**

Glass label, charge compensator oxide, density  $\rho$ , molar volume  $V_m$ , cation coordination number C.N., cation effective ionic radius  $r$ , cation field strength  $z/r^2$ , atomic packing factor  $C_g$  and glass transition temperature  $T_g$  for the eight tectosilicate glasses under study.

Glass ID	$X_{2n}^{n+}O^{2-}$	$\rho$ g.cm $^{-3}$	$V_m$ cm $^3$ .mol $^{-1}$	C.N.	$r$ Å	$z/r^2$ Å $^{-2}$	$C_g$	$T_g$ K
LA50.25	Li $_2$ O	2.431	25.91	6 [24]	0.82	1.49	0.481	922 [25]
NA50.25	Na $_2$ O	2.494	28.48	7 [26]	1.20	0.69	0.490	1074
KA50.25	K $_2$ O	2.463	32.11	9 [27]	1.60	0.39	0.528	1193
MA50.25	MgO	2.678	24.50	6 [28]	0.80	3.12	0.494	1082
CA50.25	CaO	2.690	25.85	7–8 [26,29]	1.15	1.51	0.493	1131
SA50.25	SrO	3.021	26.95	8 [30]	1.33	1.13	0.492	1152
BA50.25	BaO	3.300	28.44	8 [30]	1.50	0.89	0.489	1149 [31]
ZA50.25	ZnO	3.091	24.55	6 [24]	0.80	3.12	0.493	1022

this geometry with an accuracy of  $\pm 0.6\%$ , i.e. down to the third digit:

$$\nu = \frac{1}{2} \frac{(\nu_{B_L}^2 - 2\nu_{B_T}^2)}{(\nu_{B_L}^2 - \nu_{B_T}^2)} \quad (3)$$

The hypersonic velocities  $\nu_L$  and  $\nu_T$  were computed from the measured Brillouin shifts and the known external scattering angle  $\theta$  using Eq. (2), see Table 2. Uncertainty is approximately  $\pm 0.5\%$ , mostly arising from the initial determination of  $\theta$ .

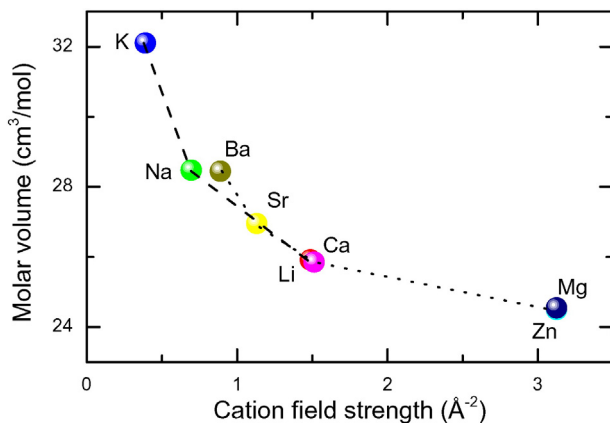
Transverse modes can be actually detected in backscattering Brillouin experiments on isotropic materials using high-NA collection optics. For a near backscattering angle  $\theta'$ , intensity of the TA modes is indeed proportional to  $\sin^2 \alpha/2$  where  $\alpha = \pi - \theta'$ . A high-NA backscattering spectrum obtained on the calcium aluminosilicate glass is shown in Fig. 4. Beside the intense LA modes, a clear signature of the TA excitations is observed with an intensity comparable to that obtained using the symmetric platelet scattering geometry. It is a very convenient way to measure Poisson's ratio for samples that cannot be easily prepared as transparent platelets. We report in Table 2 Poisson's ratio  $\nu_{bs}$  derived from the backscattering data together with those derived from the platelet geometry, showing a very good agreement. Accuracy of  $\nu_{bs}$  is about  $\pm 1\%$ .

Sound velocity data were further combined with sample density to calculate the elastic constants using the following relations, written in such a way that uncertainty calculation can be easily carried out:

$$M = C_{11} = \rho \nu_L^2 \quad (4)$$

$$G = C_{44} = \rho \nu_T^2 \quad (5)$$

$$B = \frac{M}{3} \frac{1 + \nu}{1 - \nu} \quad (6)$$



**Fig. 1.** Molar volume  $V_m$  as a function of the cation field strength  $z/r^2$ . Plotted values are labeled with the charge balancing cations. Dashed and dotted lines, linking alkali- and alkaline earth-containing glasses respectively, are guides for the eye.

$$E = 2G(1 + \nu) \quad (7)$$

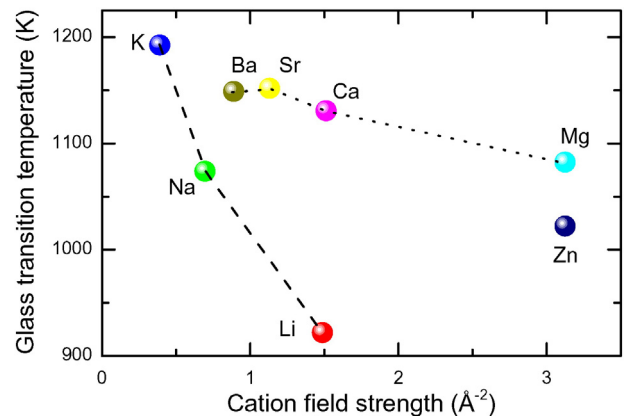
The longitudinal  $M$ , shear  $G$ , bulk  $B$ , and Young's  $E$  moduli are reported in Table 2. The overall uncertainty of the derived elastic moduli is approximately  $\pm 1\%$ . The elastic moduli compare very well with literature data for the Na [36,37] and Ca [38,39] bearing glasses whereas significant different values can be found for the Li containing glass [40]. The much lower mass density of the sample investigated in the later work,  $\rho = 2.363$  g.cm $^{-3}$ , as compared to our value  $\rho = 2.431$  g.cm $^{-3}$  that agrees with recent work [25], indicates that the data reported in [40] for LA50.25 likely refers to a glass with a slightly different composition.

The Debye temperature  $\theta_D$  can be derived from the sound velocities as well, following the standard relation:

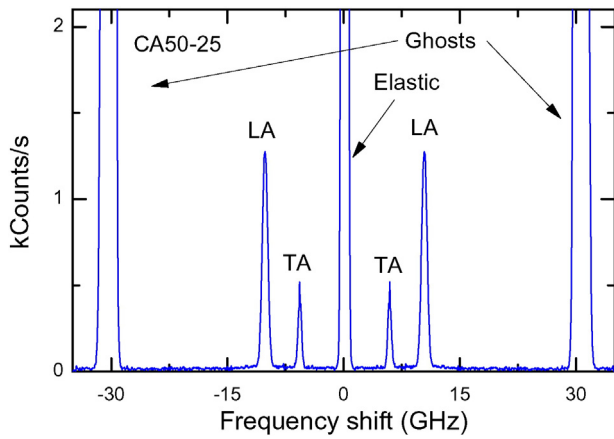
$$\theta_D = \frac{h}{k_b} \left( \frac{9N}{4\pi V_a} \right)^{1/3} \left[ \frac{1}{\nu_L^3} + \frac{2}{\nu_T^3} \right]^{-1/3} \quad (8)$$

where  $h$  is the Planck's constant,  $k_b$  the Boltzmann's constant,  $N$  the Avogadro's number, and  $V_a$  the atomic volume. The Debye temperature represents the temperature at which all vibrational modes are excited, and allows to estimate the vibrational entropy of the glass. As seen in Table 2,  $\theta_D$  increases with decreasing  $V_m$ , alkali-bearing glasses having higher Debye temperatures than alkaline earth ones. From magnesium to barium, a decrease of nearly 150 K, i.e.  $>30\%$ , is observed whereas the difference amounts to 100 K between lithium and potassium.

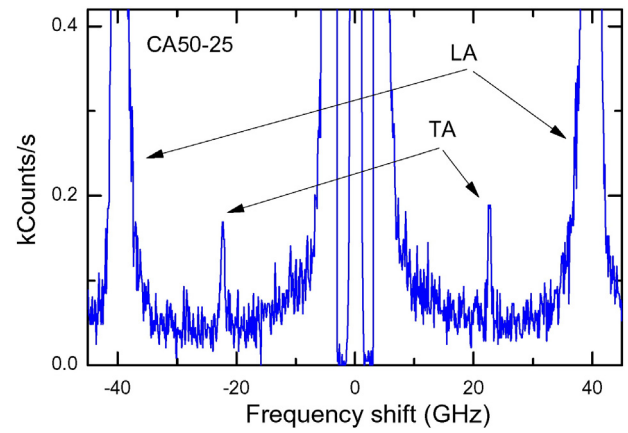
Finally, the Brillouin frequency shifts of the longitudinal modes obtained in platelet and backscattering geometries were used to estimate the refractive index  $n$  at 532 nm using Eqs. (1) and (2). The refractive index, see Table 2, roughly scales with the glass density and increases from about 1.53 for Na and K containing glasses up to about 1.62 for the barium bearing glass. The refractive index is indeed mainly governed by the mean polarisability of the ions forming the glass which generally increases with their number of electrons, i.e. a quantity



**Fig. 2.** Glass transition temperature  $T_g$  as a function of the charge balancing cation field strength  $z/r^2$ .



**Fig. 3.** Typical Brillouin scattering spectrum obtained on the calcium bearing glass in the 50° symmetric platelet geometry. LA(TA) indicate the longitudinal(transverse) modes. The central peak is the elastic scattered intensity, i.e. the Rayleigh line, whereas the outer pair of peaks arises from the Rayleigh ghosts of the first order. The spectrum was recorded in about 4 min at room temperature.



**Fig. 4.** Typical Brillouin scattering spectrum obtained on the calcium bearing glass in backscattering geometry using high NA optics, showing both longitudinal acoustic (LA) and transverse acoustic (TA) modes. The spectrum was recorded in about 4 min at room temperature.

that is directly related to the atomic mass. It is thus expected to find a good correlation between the refractive index and the glass density and not the molar volume.

#### 4. Discussion

The macroscopic elastic moduli of structural glasses are generally controlled by both the atomic density and the inter-atomic forces. As minor changes of the overall bond energies are foreseen in the investigated glass series, it is expected that atomic density governs the macroscopic elastic properties. This is illustrated in Fig. 5a–c showing the obtained elastic moduli as a function of the molar volume. Shear, bulk and Young's moduli indeed increase with increasing atomic density, i.e. with decreasing molar volume. More precisely, alkaline earth aluminosilicate glasses have slightly higher moduli than their alkali counterparts at constant molar volume, a trend which depends on the elastic modulus. While it is hardly visible for the shear modulus, it is clearly seen for the Young's modulus and becomes significant for the bulk modulus. Further, we note that the Zn-bearing glass has the highest elastic moduli of the series and follows identical trends. Finally we observe that the elastic modulus increases with increasing cation field strength as can be inferred from Figs. 1 and 5.

Conversely, an almost constant Poisson's ratio  $\nu \approx 0.234$  is obtained for the three alkali containing glasses (Fig. 6), the sodium bearing glass having the lowest value. The four alkaline earth glasses also display similar Poisson's ratio, albeit slightly higher ones,  $\nu \approx 0.265$ . Besides, the zinc containing aluminosilicate glass shows the highest Poisson's ratio  $\nu \approx 0.280$ . Whereas the magnitude of the elastic moduli is essentially governed by the atomic density in this series of tectosilicate glasses, it appears that Poisson's ratio is not. Actually, it is often assumed that

Poisson's ratio is more closely connected to the glass network connectivity governing the atomic packing factor  $C_g$  than to the atomic density or molar volume [41].  $C_g$  is the ratio between the minimum theoretical volume occupied by the ions and the corresponding effective volume of the glass:

$$C_g = \frac{1}{V_m} \sum_i V_i x_i \quad (9)$$

where

$$V_i = \frac{4}{3} \pi \mathcal{N} (x r_A^3 + y r_O^3) \quad (10)$$

is the molar volume of the  $i$ th constituent oxide of molar fraction  $x_i$  with  $A_x O_y$  chemical formula. In Eq. (10),  $r_A$  and  $r_O$  are the effective ionic radii taken from [24] for O, Si, and Al whereas  $\mathcal{N}$  is the Avogadro number. For the charge compensator cations we used the  $r$  values previously mentioned to calculate the cation field strength  $z/r^2$ .  $C_g$  values are reported in Table 1.

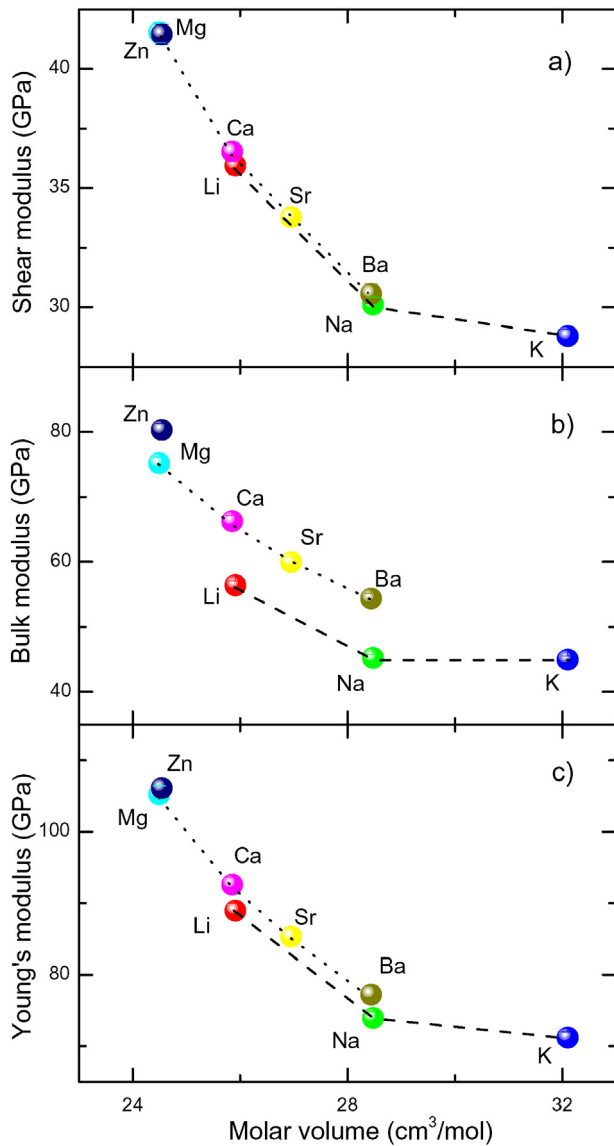
Even if the increase of  $\nu$  with  $C_g$  does not follow a one to one relation as illustrated in Fig. 7, a faint trend is observed. The modest increase of the Poisson's ratio when going from alkali to alkaline earth-bearing glasses might suggest a progressive decrease of the network dimensionality according to [41]. Recent NMR experiments [13] have indeed shown that the content of “non-stoichiometric” non-bridging oxygen, which amounts to a few percent in  $\text{XAlSiO}_4$  glasses, is governed by the charge of the cation and not its field strength as opposed to the content of VAl [42]. Alternatively, the increasing Poisson's ratio could reflect modifications of the glassy network topology. Such differences between alkali- and alkaline earth-bearing  $\text{XAlSiO}_4$  tectosilicate glasses have

**Table 2**

Longitudinal sound velocity  $v_L$ , transverse sound velocity  $v_T$ , longitudinal modulus  $M$ , shear modulus  $G$ , bulk modulus  $B$ , Young's modulus  $E$ , Poisson's ratio  $\nu$ , Poisson's ratio  $\nu_{bs}$  from backscattering data, Debye temperature  $\theta_D$ , and refractive index  $n$  at  $\lambda = 532$  nm for the aluminosilicate glasses under study. Numbers in parentheses give uncertainty of the last digit.

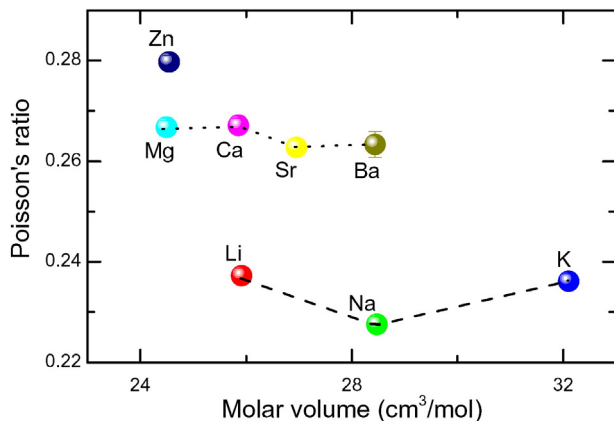
Glass ID	$v_L$ km.s <sup>-1</sup>	$v_T$ km.s <sup>-1</sup>	$M$ GPa	$G$ GPa	$B$ GPa	$E$ GPa	$\nu$	$\nu_{bs}$	$\theta_D$ K	$n$
LA50.25	6.55(3)	3.85(2)	104.3(1.0)	35.9(4)	56.4(7)	88.9(1.1)	0.237(2)	0.241(1)	550(3)	1.564(5)
NA50.25	5.85(3)	3.47(2)	85.4(0.8)	30.1(3)	45.2(6)	73.9(0.8)	0.228(2)	0.228(1)	481(2)	1.533(5)
KA50.25	5.82(3)	3.42(2)	83.4(0.8)	28.8(3)	45.0(6)	71.2(0.8)	0.236(2)	0.234(1)	455(2)	1.532(5)
MA50.25	6.98(3)	3.94(2)	130.6(1.3)	41.5(4)	75.2(9)	105.2(1.2)	0.267(1)	0.270(1)	561(3)	1.585(5)
CA50.25	6.54(3)	3.69(2)	115.0(1.1)	36.5(4)	66.3(8)	92.6(1.1)	0.267(1)	0.267(1)	516(3)	1.604(5)
SA50.25	5.90(3)	3.34(2)	105.0(1.0)	33.8(4)	59.9(7)	85.3(1.0)	0.263(1)	0.265(1)	462(2)	1.596(5)
BA50.25	5.37(3)	3.04(2)	95.1(0.9)	30.6(4)	54.4(8)	77.2(1.2)	0.263(3)	0.262(1)	413(3)	1.619(7)
ZA50.25	6.62(3)	3.66(2)	135.5(1.3)	41.4(4)	80.3(9)	106.1(1.2)	0.280(1)	0.282(1)	523(3)	1.603(5)



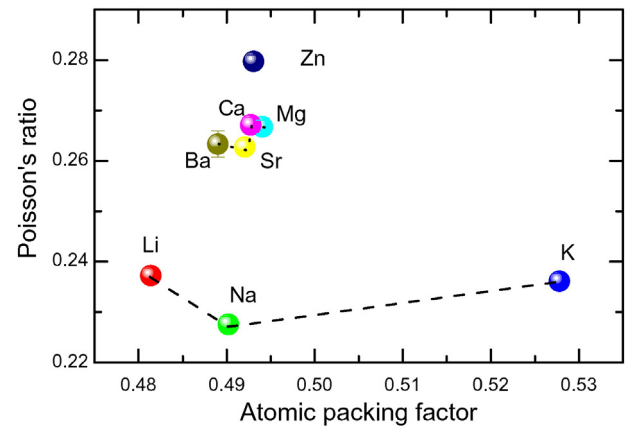


**Fig. 5.** Elastic moduli of the investigated aluminosilicate glasses as a function of the molar volume  $V_m$ : a) shear modulus  $G$ , b) bulk modulus  $B$ , and c) Young's modulus  $E$ .

been evidenced using X-ray diffraction:  $\text{NaAlSiO}_4$  glass seems mostly formed with six-membered rings containing interstitial alkali cations [4,43,44]. Substitute the alkaline earth cations for alkali ones induces



**Fig. 6.** Poisson's ratio  $\nu$  as a function of the molar volume.



**Fig. 7.** Poisson's ratio  $\nu$  as a function of the atomic packing factor.

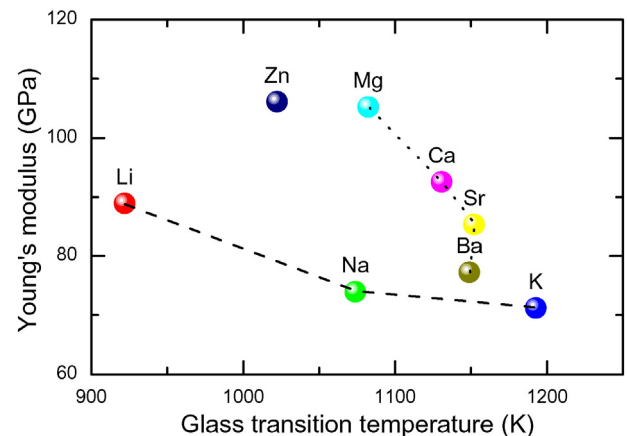
rearrangements of the aluminosilicate framework to maintain local charge balance, i.e. two aluminate tetrahedra must be close to each alkaline earth cation, thus leading to a rather different local structure containing more four-membered rings  $\text{Al}_2\text{Si}_2\text{O}_8^{2-}$  as in the  $\text{Ca}_{0.5}\text{AlSiO}_4$  case [4,43,44].

However, a striking difference between alkali- and alkaline earth-containing  $\text{XAlSiO}_4$  glasses is certainly the relation between the cation size and the compactness of the network. While the four alkaline earth-bearing glasses share very similar  $C_g$  values in reverse order of  $V_m$  and cation size  $r$ , the three alkali glasses show a large increase of  $C_g$  with increasing  $V_m$  and  $r$ . In particular, the K bearing glass displays a much higher atomic packing factor, as well as a higher molar volume, as compared to the Na glass implying a marked change in the underlying glass network topology [35].

For chemically closely related glasses, glass transition temperature is often believed to scale with elastic moduli [45]. Striking correlations between Young's modulus and  $T_g$  has been reported for example in bulk metallic glasses [46]. On the other hand, glasses formed from completely different chemical species but sharing similar stiffness can span a large range of  $T_g$ . We report in Fig. 8 the variation of  $E$  with  $T_g$  for the investigated glasses, revealing oppositely a negative correlation:  $T_g$  increases with decreasing  $E$  both for alkali- and alkaline earth-bearing glasses.

## 5. Conclusion

Charge compensated aluminosilicate glasses with the molar composition  $\text{XAlSiO}_4$  where  $\text{X} = \text{Li}, \text{Na}, \text{K}, \text{Mg}_{0.5}, \text{Ca}_{0.5}, \text{Sr}_{0.5}, \text{Ba}_{0.5}$ , and  $\text{Zn}_{0.5}$  were synthesized, characterized and investigated using Brillouin light



**Fig. 8.** Young's modulus versus glass transition temperature  $T_g$ .

scattering. We observe a concomitantly increase of atomic density and elastic moduli with increasing charge-balancing cation field strengths. It likely originates from a tighter binding of the Al-connected oxygen atoms to the lighter cations. Differently, the Poisson's ratio depends on the nature of the charge balancing cations, whether it is an alkali, an alkaline earth or a transition metal, revealing subtle changes in the topology of the aluminosilicate framework. Finally, we also report the negative correlation between the Young's modulus and the glass transition temperature in this glass series.

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