On the renormalization of the Electroweak chiral Lagrangian with a Higgs

Pedro A N Machado

in collaboration with B Gavela, K Kanshin, S Saa, S Rigolin











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What is this bump?



Is it the SM Higgs?

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Is it an elementary particle?

Are the Yukawas fundamental interactions?

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What is this bump?



Is it the SM Higgs?

Is it an elementary particle? Are the Yukawas fundamental interactions? Whatever that is, how can it be used to probe/understand BSM physics?

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Hierarchy problem



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Hierarchy problem



Thinking in terms of the running is much simpler

$$\delta m_H^2 \propto \frac{y^2}{16\pi^2} M^2 \log \frac{q^2}{M^2}$$

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New physics at high scale - Fine tuning

Is it a problem? Or is it a puzzle?

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Flavour puzzle

How can the same mechanism explain the top and the electron masses?

Moreover, flavour physics generically push up the scale of new physics a lot

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Flavour puzzle

How can the same mechanism explain the top and the electron masses?

Moreover, flavour physics generically push up the scale of new physics a lot

Are the Yukawas fundamental fields? Is there a flavour symmetry?

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Neutrino masses problem

Neutrinos oscillate, so they have mass

Mimicking the charged fermion sector, the right handed neutrino allows for a Majorana mass, which can lead to a see-saw mechanism

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Mimicking the charged fermion sector, the right handed neutrino allows for a Majorana mass, which can lead to a see-saw mechanism

The origin of neutrino masses and the nature of neutrinos is unknown

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The hierarchy puzzle is present for any scalar particle and it is reflected on its mass, particularly the higgs mass

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Neutrino masses might require new physics at very high scales that couples to the higgs (worsening the first puzzle)

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The hierarchy puzzle is present for any scalar particle and it is reflected on its mass, particularly the higgs mass

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Neutrino masses might require new physics at very high scales that couples to the higgs (worsening the first puzzle)

There is something special about scalars...

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Why do we need a higgs?



In WW scattering, the longitudinal modes amplitudes grow with energy eventually violating unitarity

The SM higgs contribution moderate this growth in such a way that unitarity is preserved

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The SM higgs contribution moderate this growth in such a way that unitarity is preserved

Deviations from the SM higgs may imply loss of unitarity, unless there is new physics to moderate the energy growth

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Vacuum stability

Having a scalar in the theory allows for a scalar potential which gets quantum corrections

In principle we can see up to which point we can extrapolate our theory

Meta-stability region up to the Planck scale

It does not tell much...



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1.5

Experimental data

Higgs couplings



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There is a gap between EW and new physics scales

The higgs is the SM one

New physics is supposed to be integrated out



Buchmuller Wyler 1986 Grzadkowski + 2010

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As we do not know which new physics is there, we write all possible operators and suppress them using a <u>dimensional counting</u>

$$\mathcal{L} = L_4 + \frac{1}{\Lambda}L_5 + \frac{1}{\Lambda^2}L_6 + \dots$$

Buchmuller Wyler 1986 Grzadkowski + 2010

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What is this counting?

The counting reflects which is the expansion we think it makes sense

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But there are other possibilities (low energy QCD, for instance)

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We only need 3 degrees of freedom to give mass to W and Z

Non-linear sigma model with f = v

Fermion masses could come from a strong sector condensate

In fact, there is no need to have a doublet – EWSB could be realized non-linearly

Most simple technicolor is severely constrained by EWPT

Weinberg 1979, Susskind 1979, Dimopoulos Susskind 1979, Callan Coleman Wess Zumino 1980, Kaplan Georgi 1984, PeskinTakeuchi 1990, Holdom Terning 1990, Golden Randall 1991

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Higgs doublet lives in G/H, but its potential vanishes at tree level

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Defining the non-linear theory $SU(2)_L \times U(1)_Y$ $UU^{\dagger} = U^{\dagger}U = 1$ $U \rightarrow LUR^{\dagger}$ $V_{\mu} = (D_{\mu}U)U^{\dagger}$ $T = U\tau^3 U^{\dagger}$

h is a singlet

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$$(2\pi)^{4} \delta^{4} (\Sigma p_{i}) \left(\frac{\pi}{f}\right)^{A} \left(\frac{\psi}{f\sqrt{\Lambda}}\right)^{B} \left(\frac{gG_{\mu}}{\Lambda}\right)^{C} \left(\frac{p}{\Lambda}\right)^{D} f^{2} \Lambda^{2}$$

Georgi Manohar 1984

 $f < \Lambda < 4\pi f$

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Georgi Manohar 1984
$$\Lambda < 4\pi f$$

Write down all invariant operators, expand in derivatives

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Thursday 18 December 14

f <

Non-linear higgs EFT

 $\mathcal{L}_0 = -V(h)$ F(h) are polynomial functions of h/v $\mathcal{F}_i(h) = 1 + 2a_ih/v + b_ih^2/v^2$

$$\mathcal{L}_2 = \frac{1}{2} \partial_\mu h \partial^\mu h \ \mathcal{F}_H(h) - \frac{v^2}{4} \operatorname{Tr}[\mathbf{V}_\mu \mathbf{V}^\mu] \ \mathcal{F}_C(h)$$

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$$\left(\operatorname{Tr}[\mathbf{V}_{\mu}\mathbf{V}^{\mu}]\right)^{2}c_{6}\mathcal{F}_{6}(h)$$

$$\operatorname{Tr}[\mathbf{V}_{\nu}\mathcal{D}_{\mu}\mathbf{V}^{\mu}]\frac{\partial^{\nu}h}{v}c_{10}\mathcal{F}_{10}(h)$$

$$\frac{\Box h \Box h}{v^2} c_{\Box H} \mathcal{F}_{\Box H}(h)$$

Appelquist Bernard PRD 1980 Longhitano PRD 1980 Longhitano NPB 1981 Appelquist Wu PRD 1993 Feruglio IJMP 1993 Alonso et al PLB 2013 Buchala et al NPB 2014

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Non-linear higgs EFT

There has been a lot of activity in this field

Full gauge-higgs basis Alonso et al PLB 2013 Gavela et al 1406.6367

Distinguishing the linear and the non-linear scenarios Brivio et al JHEP 2014

> Full basis including fermions Buchalla et al NPB 2014

(I-loop) signals at collider Delgado et al JHEP 2014

Unitarity constraints

Delgado et al 1408.1193 Espriu Mescia PRD 2014 Espriu Mescia Yencho PRD 2013

Effective Lagrangian for generic symmetry cosets Alonso et al 1409,1589

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Theoretical consistency

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Theoretical consistency

The chiral Lagrangian is renormalizable order by order

Hence, a complete $L_{d \le 4}$ basis should renormalize the $L_{d \le 2}$ Lagrangian, providing a test of the NDA prescription

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It is long known that the off-shell renormalization of the nonlinear sigma model displays apparent chiral non-invariant divergencies (NID) It has been shown that the NIDs are unphysical We would like to do the same for the EW chiral Lagrangian Charap 1970, Appelquist Bernard 1981, Kazakov+ 1977, Honerkamp 1972, ...

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Future phenomenology

The RGEs may be useful when comparing future higgs data at different energies see for instance Alonso+ 2013

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SETUP only the h – π sector of the Lagrangian (longitudinal modes of gauge bosons) g, g' = 0 no custodial breaking terms renormalization up to 4 legs <u>General U matrix parametrization</u> Off-shell amplitudes

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U parametrization: we only need to satisfy $UU^{\dagger} = U^{\dagger}U = I$

$$\mathbf{U} = 1 - \frac{\boldsymbol{\pi}^2}{2v^2} - \left(\boldsymbol{\eta} + \frac{1}{8}\right) \frac{\boldsymbol{\pi}^4}{v^4} + \frac{i\boldsymbol{\tau}\boldsymbol{\pi}}{v} \left(1 + \boldsymbol{\eta}\frac{\boldsymbol{\pi}^2}{v^2}\right) + O(\boldsymbol{\pi}^5)$$
$$\eta = 0 \Rightarrow \mathbf{U} = \sqrt{1 - \boldsymbol{\pi}^2/v^2} + i\boldsymbol{\tau}\boldsymbol{\pi}/v$$
$$\eta = -1/6 \Rightarrow \mathbf{U} = e^{i\boldsymbol{\tau}\boldsymbol{\pi}/v}$$

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All physical quantities are independent of η

Weinberg 1968

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I-point function



Boring... just get a source counterterm to cancel the tadpole $\pi \xrightarrow{\rightarrow} \pi$



2

3

2-point function



$$\Pi_{\text{div}}^{ij}(p^2) = \left[p^2 \left(a_C^2 - b_C \right) \frac{m_h^2}{v^2} + p^4 \frac{a_C^2}{v^2} \right] \delta_{ij}$$
$$\Pi_{ctr}^{ij}(p^2) = \left[p^2 \delta_\pi - p^4 \frac{4}{v^2} \left(\delta c_9 - \frac{\delta v^2}{v^2} \right) \right] \delta_{ij}$$

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2

2

2-point function



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2

2

2-point function



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3- and 4-point functions



I am not going to write down all formulas, ok?

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3- and 4-point functions

Due to the off-shell renormalization, we expect a long list of required operators In fact, we get ALL h – π invariant operators in L4

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We agree with Georgi-Manohar NDA

We find explicitly that physical quantities do not depend on η

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There are apparent non-invariant divergencies involving the higgs

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 $-\left(\frac{3}{2}-5\eta\right)a_C\Delta_{\varepsilon}\,\boldsymbol{\pi}\Box\boldsymbol{\pi}\Box h$

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$$- \left(\frac{3}{2} - 5\eta\right) a_C \Delta_{\varepsilon} \, \pi \Box \pi \Box h \qquad - \left(9\eta^2 + 5\eta + \frac{3}{4}\right) \frac{\Delta_{\varepsilon}}{v^4} (\pi \Box \pi)^2, \\ - (2a_C^2 - b_C) \left(\frac{3}{2} - 5\eta\right) \frac{\Delta_{\varepsilon}}{v^4} \, \pi \Box \pi \, h \Box h \qquad - \left[1 + 4\eta + \left(\frac{1}{2} + \eta\right) a_C^2\right] \frac{\Delta_{\varepsilon}}{v^4} (\pi \Box \pi) (\partial_{\mu} \pi \partial^{\mu} \pi), \\ - (a_C^2 - b_C) \left(\frac{3}{2} - 5\eta\right) \frac{\Delta_{\varepsilon}}{v^4} \, \pi \Box \pi \, \partial_{\mu} h \partial^{\mu} h \qquad - 2\eta^2 \frac{\Delta_{\varepsilon}}{v^4} \, \pi^2 (\Box \pi)^2, \\ + 2a_C^2 \left(\frac{3}{2} - 5\eta\right) \frac{\Delta_{\varepsilon}}{v^4} \, \pi \partial_{\mu} \pi \, \partial^{\mu} h \Box h \qquad - 2\eta \left(a_C^2 - 1\right) \frac{\Delta_{\varepsilon}}{v^4} (\Box \pi \partial_{\mu} \pi) (\pi \partial^{\mu} \pi).$$

These terms do not respect chiral invariance!!! How do we deal with it?

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There are many methods to deal with the NIDs

Proper quantization using the Hamiltonian formalist which yields non-covariant Feynman rules Gerstein Jackiw Weinberg Lee 1971

Modified background field method Honerkamp 1972 Kazakov Peryushin Pushkin 1976

Field redefinition

Appelquist Bernard 1981

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Lagrangians related by local field redefinitions, even involving derivatives or other fields, are equivalent Ostrogradsky 1850, Grosse-Knetter 1993, Arzt 1993, Scherer Fearing 1994

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Lagrangians related by local field redefinitions, even involving derivatives or other fields, are equivalent Ostrogradsky 1850, Grosse-Knetter 1993, Arzt 1993, Scherer Fearing 1994

Hence, if we redefine the π field $\pi \to \pi f(\pi, \partial_{\mu}\pi, h, \partial_{\mu}h, \dots), \quad f(0) = 1$ in such a way that $\mathcal{L}(\pi, \partial_{\mu}\pi, h, \partial_{\mu}h) \to \mathcal{L}(\pi, \partial_{\mu}\pi, h, \partial_{\mu}h) + \Delta \mathcal{L}$ the Δ L term in the Lagrangian is not physical

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With this redefinition

$$\pi_{i} \to \pi_{i} \left(1 + \frac{\alpha_{1}}{2v^{4}} \boldsymbol{\pi} \Box \boldsymbol{\pi} + \frac{\alpha_{2}}{2v^{4}} \partial_{\mu} \boldsymbol{\pi} \partial^{\mu} \boldsymbol{\pi} + \frac{\beta}{2v^{3}} \Box h + \frac{\gamma_{1}}{2v^{4}} h \Box h + \frac{\gamma_{2}}{2v^{4}} \partial_{\mu} h \partial^{\mu} h \right) \\ + \frac{\alpha_{3}}{2v^{4}} \Box \pi_{i} (\boldsymbol{\pi} \boldsymbol{\pi}) + \frac{\alpha_{4}}{2v^{4}} \partial_{\mu} \pi_{i} (\boldsymbol{\pi} \partial^{\mu} \boldsymbol{\pi})$$

we can absorb all NIDs

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With this redefinition

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we can absorb all NIDs

Therefore, chiral symmetry is never broken: the non-invariant terms are actually "zero" (inside a path integral)

This should be equivalent to use the equations of motion

(but a bit more elegant, in my opinion)

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RGEs

$$16\pi^{2} \frac{d}{d \ln \mu} \lambda = \lambda \left[26a_{H} \frac{\mu_{3}}{v} + \left(14b_{H} - 82a_{H}^{2} \right) \frac{m_{h}^{2}}{v^{2}} \right] - \frac{3}{2} \lambda^{2} + 12 \left(b_{H} - 6a_{H}^{2} \right) \frac{\mu_{3}^{2}}{v^{2}} + 48a_{H} \left(8a_{H}^{2} - 3b_{H} \right) \mu_{3} \frac{m_{h}^{2}}{v^{3}} - 6 \left(80a_{H}^{4} - 48b_{H}a_{H}^{2} + 3b_{H}^{2} \right) \frac{m_{h}^{4}}{v^{4}}.$$

$$16\pi^2 \frac{d}{d\ln\mu} b_H = b_H \left[20a_H \frac{\mu_3}{v} - \frac{3}{2}\lambda + \left(-a_C^2 + b_C - 87a_H^2 \right) \frac{m_h^2}{v^2} \right] - 42\frac{\mu_3}{v}a_H^3 + \frac{13}{2}\lambda a_H^2 + \left(7b_H^2 + 120a_H^4 \right) \frac{m_h^2}{v^2} .$$

$$16\pi^2 \frac{d}{d\ln\mu} c_6 = -\frac{1}{24} \left[2 + 2a_C^4 + 3b_C^2 - a_C^2 \left(-8 + 6b_C \right) \right]$$

Although in the SM limit the RGEs for BSM operators do not vanish, BSM contributions cancel when calculating physical quantities!

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Off-shell one loop renormalization of the $h-\pi$ non-linear Lagrangian

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Off-shell one loop renormalization of the h – π non-linear Lagrangian

We found new NIDs and we provided a consistent way of dealing with them

Chiral symmetry is not broken

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RGEs might be important when higgs measurements get more precise

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Thanks!

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