# Tools and ideas for LHC phenomenology 

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## legacy of LHC Run I

ATLAS SUSY Searches* - 95\% CL Lower Limits

|  | IS: Feb 2015 |
| :---: | :---: |
| Model |  |
| 9OO©© | MSUGRA/CMSSM |
|  | $\tilde{q} \tilde{q}, \tilde{q} \rightarrow \tilde{\chi}_{1}^{0}$ |
|  | $\tilde{q} \tilde{q} \gamma, \tilde{q} \rightarrow \chi_{1}^{0} \hat{\chi}_{1}^{0}$ (compressed) |
|  | $\bar{g} \dot{g}, \underline{g} \rightarrow q \bar{q} \hat{q}_{1}^{0}$ |
|  | $\tilde{g} \tilde{g}, \underline{g} \rightarrow q q \tilde{1}_{1}^{ \pm} \rightarrow q q W^{ \pm} \tilde{\chi}_{1}^{0}$ |
|  | $\underline{g} \tilde{g}, \tilde{g} \rightarrow q q(t / / \ell v / v v)_{1}^{0}$ |
| $\begin{aligned} & 0 \\ & \frac{3}{5} \\ & \frac{3}{U} \\ & \text { E } \end{aligned}$ | GMSB ( $\check{\ell} \mathrm{NLSP}$ ) |
|  | GGM (bino NLSP) |
|  | GGM (wino NLSP) |
|  | GGM (higgsino-bino NLSP) |
|  | GGM (higgsino NLSP) |
|  | Gravitino LSP |

$\sqrt{s}=7 \mathrm{TeV}$
full data
$\sqrt{5}=8 \mathrm{TeV}$
partial data partial data
$\sqrt{s}=8 \mathrm{TeV}$
full data

ATLAS Preliminary $\sqrt{s}=7,8 \mathrm{TeV}$
$m(\vec{g})=m(\vec{g})$
$m\left(X_{1}^{0}\right)=0 \operatorname{GeV}, m\left(I^{\mathrm{s}} \operatorname{gen} . \overline{\mathrm{q}}\right)=m\left(2^{\mathrm{d}} \operatorname{gen} . \overline{\mathrm{q}}\right)$ $m(\bar{y})-m\left(x_{1}^{0}\right)=m(c)$ $m\left(\tilde{C}_{1}^{0}\right)=0 \mathrm{GeV}$ $\mathrm{m}\left(\vec{X}_{1}^{0}\right)<300 \mathrm{GeV}, \mathrm{m}\left(\tilde{X}^{ \pm}\right)=0.5\left(\mathrm{~m}\left(\tilde{X}_{1}^{(1)}\right)+\mathrm{m}(\vec{g})\right)$ $m\left(\hat{X}_{1}^{0}\right)=0 \mathrm{GeV}$
$\tan \beta>20$
$m\left(X_{1}^{0}\right)>50 \mathrm{GeV}$
$m\left(X_{1}^{0}\right)>50 \mathrm{GeV}$
$m\left(X_{1}^{0}\right)>220 \mathrm{GeV}$ $m(N L S P)>200 \mathrm{GeV}$ $m(\bar{G})>1.8 \times 10^{-4} \mathrm{eV}, m(\tilde{g})=m(\tilde{q} \tilde{\tilde{q}}=1.5 \mathrm{TeV}$

Mass scale [TeV]

- so far no sign of new Physics at the TeV scale from direct searches


## legacy of LHC Run I



ATLAS Preliminary Total uncertainty


- so far no sign of new Physics at the TeV scale from direct searches
- Higgs couplings have started to be measured: SM-like values, within 20-30 \%


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ATLAS SUSY Searches* - 95\% CL Lower Limit


- so far no sign of new Physics at the TeV scale from direct searches
- Higgs couplings have started to be measured: SM-like values, within 20-30 \%
- Situation will hopefully change at 13-14 TeV. Otherwise BSM hints likely from:
- small deviations from SM backgrounds
- indirect searches
[Higgs couplings, precise extraction of SM parameters]


## legacy of LHC Run I

## ATLAS Preliminary

$\mathrm{m}_{\mathrm{H}}=125.36 \mathrm{GeV}$


ATLAS SUSY Searches* - 95\% CL Lower Limit
Status: Feb 2015

require accurate understanding of signals and backgrounds:喔 "precision Physics"

## Where are QCD precision and MC important?



- $s$-channel resonance "easy" to discover; Higgs discovery in $\gamma \gamma$ and $Z Z$ belongs to 1
- Some analysis techniques (e.g. 2 ) heavily relies on using MC event generators to separate signal and backgrounds
- MC very often needed also in more standard analysis...


## Where are QCD precision and MC important?




- For 3 and 4 , need to control as much as possible QCD effects (i.e. rates and shapes, and also uncertainties!).
- Similar issues when extracting a SM parameters very precisely (e.g. the $W$ mass).


## Where are QCD precision and MC important?




- at some level, MC event generators enter in almost all experimental analyses
precise tools $\Rightarrow$ smaller uncertainties on measured quantities $\Downarrow$
"small" deviations from SM accessible


## Event generators: what they are?

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- collide non-elementary particles
- we detect $e, \mu, \gamma$, hadrons, "missing energy"
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- realistically
- precisely
- from first principles

[sherpa's artistic view]


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$\Rightarrow$ full event simulation needed to:
- compare theory and data
- estimate how backgrounds affect signal region
- test/build analysis techniques
soner or later, at some point a MC is used...

[sherpa's artistic view]


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non-perturbative model, tuned on $e^{+} e^{-}$data all stages: QCD

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| hard scattering |
| :---: |
| $\Lambda_{\mathrm{QCD}} \ll \mu \approx Q$ |

perturbation theory

| parton shower |
| :--- |
| $\Lambda_{\mathrm{QCD}}<\mu<Q$ |
| hierarchy of scales |
| . resummation of large |
| logarithms |
| hadronisation |
| $\mu \approx \Lambda_{\mathrm{QCD}}$ |

non-perturbative model, tuned on $e^{+} e^{-}$data

```
all stages: QCD
```


## Event generators: what's the output?

- in practice: momenta of all outgoing leptons and hadrons:

| IHEP | ID | IDPDG IST | MO1 | MO2 | DA1 | DA2 | P-X | $P-Y$ | P-Z | ENERGY |  |
| ---: | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 31 | NU_E | -11 | 1 | 30 | 22 | 0 | 0 | -22.80 | 2.59 | -232.4 | 233.6 |
| 32 | E+ | 321 | 1 | 109 | 9 | 0 | 0 | -1.66 | 1.26 | 1.3 | 2.5 |
| 148 | K+ | 111 | 1 | 111 | 9 | 0 | 0 | -0.01 | 0.05 | 11.4 | 11.4 |
| 151 | PIO | 211 | 1 | 111 | 9 | 0 | 0 | -0.19 | -0.13 | 2.0 | 2.0 |
| 152 | PI+ | -211 | 1 | 112 | 9 | 0 | 0 | 0.84 | -1.07 | 1626.0 | 1626.0 |
| 153 | PI- | 321 | 1 | 112 | 9 | 0 | 0 | 0.48 | -0.63 | 945.7 | 945.7 |
| 154 | K+ | 111 | 1 | 113 | 9 | 0 | 0 | -0.37 | -1.16 | 64.8 | 64.8 |
| 155 | PIO | -211 | 1 | 113 | 9 | 0 | 0 | -0.20 | -0.02 | 3.1 | 3.1 |
| 156 | PI- | 111 | 1 | 114 | 9 | 0 | 0 | -0.17 | -0.11 | 0.2 | 0.3 |
| 158 | PIO | 111 | 1 | 115 | 18 | 0 | 0 | 0.18 | -0.74 | -267.8 | 267.8 |
| 159 | PIO | -211 | 1 | 115 | 18 | 0 | 0 | -0.21 | -0.13 | -259.4 | 259.4 |
| 160 | PI- | 2112 | 1 | 116 | 23 | 0 | 0 | -8.45 | -27.55 | -394.6 | 395.7 |
| 161 | N | -2112 | 1 | 116 | 23 | 0 | 0 | -2.49 | -11.05 | -154.0 | 154.4 |
| 162 | NBAR | 111 | 1 | 117 | 23 | 0 | 0 | -0.45 | -2.04 | -26.6 | 26.6 |
| 163 | PIO | 111 | 1 | 117 | 23 | 0 | 0 | 0.00 | -3.70 | -56.0 | 56.1 |
| 164 | PIO | 321 | 1 | 119 | 23 | 0 | 0 | -0.40 | -0.19 | -8.1 | 8.1 |
| 167 | K+ | -2212 | 1 | 130 | 9 | 0 | 0 | 0.10 | 0.17 | -0.3 | 1.0 |

1. review how these tools work
2. discuss how their accuracy can be improved
3. show recent "NNLO matched to parton showers" results (NNLOPS)

parton showers and fixed order

## Parton showers I

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3. soft-collinear emissions are ennhanced:

$$
\frac{1}{\left(p_{1}+p_{2}\right)^{2}}=\frac{1}{2 E_{1} E_{2}(1-\cos \theta)}
$$

4. in soft-collinear limit, factorization properties of QCD amplitudes


$$
\begin{aligned}
\left|\mathcal{M}_{n+1}\right|^{2} d \Phi_{n+1} \rightarrow\left|\mathcal{M}_{n}\right|^{2} d \Phi_{n} & \frac{\alpha_{\mathrm{S}}}{2 \pi} \frac{d t}{t} P_{q, q g}(z) d z \frac{d \varphi}{2 \pi} \\
z=k^{0} /\left(k^{0}+l^{0}\right) & \text { quark energy fraction } \\
t=\left\{(k+l)^{2}, l_{T}^{2}, E^{2} \theta^{2}\right\} & \text { splitting hardness } \\
P_{q, q g}(z)=C_{\mathrm{F}} \frac{1+z^{2}}{1-z} & \text { AP splitting function }
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probabilistic interpretation!

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$$


probabilistic interpretation! [notice: $\alpha_{\mathrm{S}} L^{2}$ ]

## Parton showers II

5. dominant contributions for multiparticle production due to strongly ordered emissions

$$
t_{1}>t_{2}>t_{3} \ldots
$$

6. at any given order, we also have virtual corrections: include them with the same approximation


- LL virtual contributions: Sudakov form factor for each internal line:

$$
\Delta_{a}\left(t_{i}, t_{i+1}\right)=\exp \left[-\sum_{(b c)} \int_{t_{i+1}}^{t_{i}} \frac{d t^{\prime}}{t^{\prime}} \int \frac{\alpha_{s}\left(t^{\prime}\right)}{2 \pi} P_{a, b c}(z) d z\right]
$$

- $\Delta_{a}$ corresponds to the probability of having no resolved emission between $t_{i}$ and $t_{i+1}$ off a line of flavour $a$
[1/8 resummation of collinear logarithms
[very soff/collinear emissions are suppressed - all order effect!]


## Parton showers: summary

$$
d \sigma_{\mathrm{SMC}}=\underbrace{\left|\mathcal{M}_{B}\right|^{2} d \Phi_{B}}_{d \sigma_{B}}\{
$$



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d \sigma_{\mathrm{SMC}}=\underbrace{\left|\mathcal{M}_{B}\right|^{2} d \Phi_{B}}_{d \sigma_{B}}\left\{\Delta\left(t_{\mathrm{max}}, t_{0}\right)\right.
$$



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d \sigma_{\mathrm{SMC}}=\underbrace{\left|\mathcal{M}_{B}\right|^{2} d \Phi_{B}}_{d \sigma_{B}}\{\Delta\left(t_{\max }, t_{0}\right)+\Delta\left(t_{\max }, t\right) \underbrace{d \mathcal{P}_{\mathrm{emis}}(t)}_{\frac{\alpha_{s}}{2 \pi} \frac{1}{t} P(z) d \Phi_{r}}
$$



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$$



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- A parton shower changes shapes, not the overall normalization, which stays LO (unitarity)


## Do they work?



plot from [Gianotti,Mangano 0504221]

- ok when observables dominated by soft-collinear radiation
- not surprisingly, they fail when looking for hard multijet kinematics
- they are only LO+LL accurate (whereas we want (N)NLO QCD corrections)
$\Rightarrow$ Not enough if interested in precision (10\% or less), or in multijet regions


## Next-to-Leading Order

$\alpha_{\mathrm{S}} \sim 0.1 \Rightarrow$ to improve the accuracy, use exact perturbative expansion

$$
d \sigma=d \sigma_{\mathrm{LO}}+\left(\frac{\alpha_{\mathrm{S}}}{2 \pi}\right) d \sigma_{\mathrm{NLO}}+\left(\frac{\alpha_{\mathrm{S}}}{2 \pi}\right)^{2} d \sigma_{\mathrm{NNLO}}+\ldots
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$$
d \sigma=d \Phi_{n}\{\underbrace{B\left(\Phi_{n}\right)}_{\mathrm{LO}}
$$



$$
\frac{\alpha_{s}}{2 \pi}[\underbrace{V\left(\Phi_{n}\right)+R\left(\Phi_{n+1}\right) d \Phi_{r}}_{\mathrm{NLO}}]
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- first order where rates are reliable
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## When NNLO is needed?

- NLO corrections large
- very high-precision needed



## NLO

$\checkmark$ precision
$\checkmark$ nowadays this is the standard
$X$ limited multiplicity
$X$ (fail when resummation needed)

## parton showers

$\checkmark$ realistic + flexible tools
$\checkmark$ widely used by experimental coll's
$X$ limited precision (LO)
$X$ (fail when multiple hard jets)
㖪 can we merge them and build an NLOPS generator?
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$\checkmark$ many proposals, 2 well-established methods available to solve this problem: MC@NLO and POWHEG
[Frixione-Webber '03, Nason '04]

## matching NLO and PS

- POWHEG (POsitive Weight Hardest Emission Generator)


## NLOPS: POWHEG I

$$
d \sigma_{\mathrm{POW}}=d \Phi_{n} \quad \bar{B}\left(\Phi_{n}\right) \quad\left\{\Delta\left(\Phi_{n} ; k_{\mathrm{T}}^{\mathrm{min}}\right)+\Delta\left(\Phi_{n} ; k_{\mathrm{T}}\right) \frac{\alpha_{s}}{2 \pi} \frac{R\left(\Phi_{n}, \Phi_{r}\right)}{B\left(\Phi_{n}\right)} d \Phi_{r}\right\}
$$

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B\left(\Phi_{n}\right) \Rightarrow \bar{B}\left(\Phi_{n}\right)=B\left(\Phi_{n}\right)+\frac{\alpha_{s}}{2 \pi}\left[V\left(\Phi_{n}\right)+\int R\left(\Phi_{n+1}\right) d \Phi_{r}\right]-
$$

$$
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$$

$$
\left(\frac{\sigma^{66}}{\sim \Delta\left(t_{\mathrm{m}}, t\right) \Rightarrow \Delta\left(\Phi_{n} ; k_{\mathrm{T}}\right)=\exp \left\{-\frac{\alpha_{s}}{2 \pi} \int \frac{R\left(\Phi_{n}, \Phi_{r}^{\prime}\right)}{B\left(\Phi_{n}\right)} \theta\left(k_{\mathrm{T}}^{\prime}-k_{\mathrm{T}}\right) d \Phi_{r}^{\prime}\right\}}\right.
$$

$$
d \sigma_{\mathrm{POW}}=d \Phi_{n} \bar{B}\left(\Phi_{n}\right)\left\{\Delta\left(\Phi_{n} ; k_{\mathrm{T}}^{\mathrm{min}}\right)+\Delta\left(\Phi_{n} ; k_{\mathrm{T}}\right) \frac{\alpha_{s}}{2 \pi} \frac{R\left(\Phi_{n}, \Phi_{r}\right)}{B\left(\Phi_{n}\right)} d \Phi_{r}\right\}
$$

[ $+p_{\mathrm{T}}$-vetoing subsequent emissions, to avoid double-counting]

- inclusive observables: @NLO
- first hard emission: full tree level ME

This is "NLOPS"

- (N)LL resummation of collinear/soft logs
- extra jets in the shower approximation


## NLOPS: POWHEG II

$$
d \sigma_{\mathrm{POW}}=d \Phi_{n} \bar{B}\left(\Phi_{n}\right)\left\{\Delta\left(\Phi_{n} ; k_{\mathrm{T}}^{\min }\right)+\Delta\left(\Phi_{n} ; k_{\mathrm{T}}\right) \frac{\alpha_{s}}{2 \pi} \frac{R\left(\Phi_{n}, \Phi_{r}\right)}{B\left(\Phi_{n}\right)} d \Phi_{r}\right\}
$$

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## POWHEG BOX

[Alioli,Nason,Oleari,ER '10]

- large library of SM processes, (largely) automated
- widely used by LHC collaborations and other theorists
- not really a closed chapter; some important issues are still to be addressed...


...a couple of possible BSM applications...


## $t \bar{t}$ and top-mass measurement

- Improvement on measurement of the top-mass at the LHC will probably come from combination of different strategies: total x -section, $t \bar{t}+$ jet, leptonic spectra, $b \ell$ endpoint,... [see e.g. TOP LHC Working Group or MITP Workshop 2014]
- Some techniques rely on looking into the kinematics of visible particles from top-decay
- Important that simulations are very accurate, and associated errors are quantified: recently, NLO+PS with NLO in production and decay
[Campbell,Ellis,Nason,ER '14]


plot from [Giudice et al. '13]

$$
m_{t} \approx 173 \pm 1 \mathrm{GeV}
$$

## BSM example II: LHC and Dark-Matter searches





## BSM example II: LHC and Dark-Matter searches

- studied QCD corrections to monojet searches
[Haisch,Kahlhoefer,ER '13]

- ATLAS and CMS cuts are such that a large fraction of events has 2 or more jets
- for some DM-SM interactions, using VBF cuts: [Haisch,Hibbs,ER '13, see also Cotta,Hewett et al. '13]

$N L O+P S$ merging and NNLO+PS


## NNLO+PS: why and where?

NLO(+PS) not always enough: NNLO needed when

1. large NLO/LO "K-factor"
[as in Higgs Physics]
2. very high precision needed
[e.g. Drell-Yan, top pairs]

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Q: can we merge NNLO and PS?

[Anastasiou et al., '03]
哏
ise important for precision studies for several processes

- method presented here: based on POWHEG+MiNLO, used so far for
- Higgs production
[Hamilton,Nason,ER,Zanderighi, 1309.0017]
- neutral \& charged Drell-Yan


## towards NNLO+PS

- what do we need and what do we already have?

|  | H (inclusive) | $\mathrm{H}+\mathrm{j}$ (inclusive) | $\mathrm{H}+2 \mathrm{j}$ (inclusive) |
| :---: | :---: | :---: | :---: |
| $\mathrm{H} @$ NLOPS | NLO | LO | shower |
| HJ @ NLOPS | $/$ | NLO | LO |
|  |  |  |  |
| H @ NNLOPS | NNLO | NLO | LO |

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| HJ @ NLOPS | I | NLO | LO |
| H-HJ @ NLOPS | NLO | NLO | LO |
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傕 a merged $\mathrm{H}-\mathrm{HJ}$ generator is almost OK

- many of the multijet NLO+PS merging approaches work by combining 2 (or more) NLO+PS generators, introducing a merging scale*
- POWHEG + MiNLO [Multiscale Improved NLO].
[Hamilton et al. '12]
No need of merging scale: it extends the validity of a NLO+PS computation with jets in the final state to phase-space regions where jets become unresolved

[^0]
## NLOPS merging \& BSM




- left: LO+PS
- right: NLO+PS merging


## POWHEG $\rightarrow$ MiNLO $\rightarrow$ NNLO+PS

Higgs at NNLO:

\# loops: 0 ( 1

\# loops: $0 \quad 1$

\# loops:

## POWHEG $\rightarrow$ MiNLO $\rightarrow$ NNLO+PS

Higgs at NNLO:


\# loops: 01

(a) 1 and 2 jets: POWHEG $\mathrm{H}+1 \mathrm{j}$

## POWHEG $\rightarrow$ MiNLO $\rightarrow$ NNLO+PS

Higgs at NNLO:

(b) - integrate down to $q_{T}=0$ with MiNLO

- "Improved MiNLO" allows to build a H-HJ @ NLOPS generator
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MiNLO

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MiNLO
"Improved" MiNLO \& NLOPS merging
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Higgs at NNLO+PS: details

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Higgs at NNLO+PS: details

## H@NNLOPS (fully incl.)

- NNLO with $\mu=m_{H} / 2$, HJ-MiNLO "core scale" $m_{H}$
- $\left(7_{\mathrm{Mi}} \times 3_{\mathrm{NN}}\right)$ pts scale var. in NNLOPS, 7 pts in NNLO



Notice: band is $10 \%$ (at NLO would be $\sim 20-30 \%$ )
[Until and including $\mathcal{O}\left(\alpha_{\mathrm{S}}^{4}\right)$, PS effects don't affect $y_{H}$ (first 2 emissions controlled properly at $\mathcal{O}\left(\alpha_{\mathrm{S}}^{4}\right)$ by MiNLO+POWHEG)]

## H@NNLOPS $\left(p_{T}^{H}\right)$




- HqT: NNLL+NNLO, $\mu_{R}=\mu_{F}=m_{H} / 2[7 \mathrm{pts}], \quad Q_{\mathrm{res}} \equiv m_{H} / 2$
[HqT, Bozzi et al.]
$\checkmark$ uncertainty bands of HqT contain nNLOPS at low-/moderate $p_{T}$
- very good agreement with HqT resummation
["~ expected", since $Q_{\mathrm{res}} \equiv m_{H} / 2$, and $\beta=1 / 2$ ]


## H@NNLOPS ( $\left.p_{T}^{j_{1}}\right)$

哏 Separation of $H \rightarrow W W$ from $t \bar{t}$ bkg: x-sec binned in $N_{\text {jet }}$
0 -jet bin $\Leftrightarrow$ jet-veto accurate predictions needed !




$$
\varepsilon\left(p_{\mathrm{T}, \text { veto }}\right)=\frac{\Sigma\left(p_{\mathrm{T}, \text { veto }}\right)}{\sigma^{\text {tot }}}=\frac{1}{\sigma^{\text {tot }}} \int d \sigma \theta\left(p_{\mathrm{T}, \text { veto }}-p_{\mathrm{T}}^{\mathrm{j}_{1}}\right)
$$

- JetVHeto: NNLL resum, $\mu_{R}=\mu_{F}=m_{H} / 2$ [7pts], $\quad Q_{\text {res }} \equiv m_{H} / 2$, (a)-scheme only [JetVHeto, Banfi et al.]
- nice agreement, differences never more than 5-6 \%


## Drell-Yan @NNLOPS



....measure $W$ mass very precisely....

## consistency of SM



## Conclusions and Outlook

- Especially in absence of very clear singals of new-physics, accurate tools are needed for LHC phenomenology
- In the last decade, impressive amount of progress: new ideas, and automated tools
$\Rightarrow$ briefly reviewed how Event Generators work, and how they can be upgraded to NLO
$\Rightarrow$ shown results of merging NLOPS for different jet-multiplicities without merging scale
$\Rightarrow$ shown first working examples of NNLOPS

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[^0]:    *[Hoeche,Krauss, et al.,1207.5030] [Frederix,Frixione,1209.6215] [Lonnblad,Prestel,1211.7278] [Platzer, 1211.5467] [Alioli,Bauer, et al.,1211.7049] ...

