

Cosmological relaxation of the EW scale

Giuliano Panico

IFAE, Barcelona

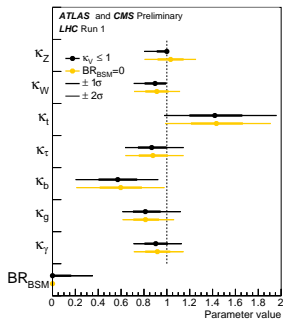
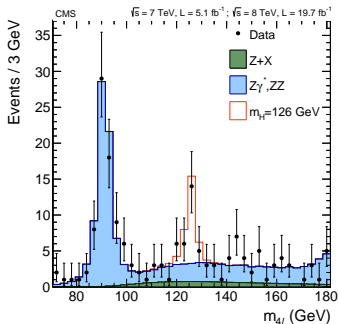
Montpellier – 15 October 2015

based on **J.R. Espinosa, C. Grojean, G. P., A. Pomarol,
O. Pujolàs, G. Servant** arXiv:1506.09217

Introduction

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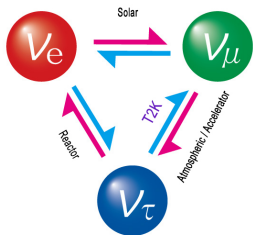
The Higgs discovery and the recent LHC measurements confirm that the Standard Model (i.e. the **Higgs mechanism**) correctly describes the main features of the **EW Symmetry Breaking** dynamics



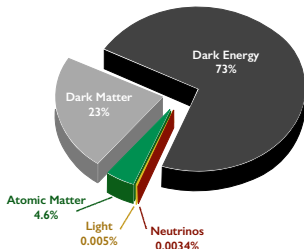
Introduction

The SM is not a complete theory, several phenomena unexplained

- origin of neutrino masses
- dark matter
- full description of gravity
- ...



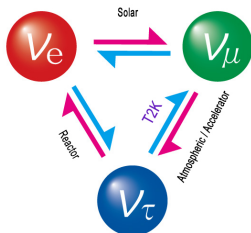
Neutrino oscillation between three generations



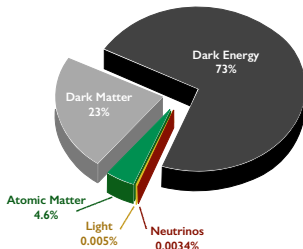
Introduction

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Neutrino oscillation between three generations



More fundamental theory necessarily present!

Introduction: the Hierarchy Problem

Obstruction to get a **predictive** extension of the SM:
the Hierarchy Problem

- ▶ the Higgs mass is highly sensitive to new physics
- ▶ its **natural** value of m_h is of the order of the new-physics scale Λ_{NP}

$$\delta m_h^2|_{1-loop} \sim \text{---} h \text{---} \begin{array}{c} \text{top} \\ \circlearrowleft \\ \text{top} \end{array} \text{---} h \text{---} \sim -\frac{y_{top}^2}{8\pi^2} \Lambda_{NP}^2 \gg (125 \text{ GeV})^2$$

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- ▶ **huge cancellation** needed to keep the Higgs mass small

$$m_h^2 = m_h^2|_{bare} + \delta m_h^2|_{1-loop} = (125 \text{ GeV})^2$$

▣➡ **loss of predictivity!**

Introduction: the Hierarchy Problem

Is the Higgs mass really **unnatural**?

- ▶ look for extensions of the SM that avoid the Hierarchy Problem

Introduction: the Hierarchy Problem

The origin of the **Hierarchy problem** can be equivalently understood as the requirement that Higgs potential satisfies two conditions near the same point

- (i) a zero of the first derivative
(local minimum)
- (ii) a zero of the second derivative
(Higgs mass and EW scale much smaller than the overall scale,
 $m_h, v \ll \Lambda$)

In a generic potential a **fine-tuning** is required to obtain the two conditions simultaneously.

Introduction: Solutions of the Hierarchy Problem

“Classical” mechanisms to solve the Hierarchy problem

- ▶ **New physics at the TeV scale** stabilizes the EW scale
(eg. low-scale Supersymmetry, Composite Higgs, ...)
 - Avoid condition (ii) by assuming that $\Lambda \sim v \sim m_h$

$$\delta m_h^2|_{1-loop} \sim \text{h} \text{---} \text{loop}(top) \text{---} \text{h} + \text{h} \text{---} \text{NP} \text{---} \text{h} \sim -\frac{y_{top}^2}{8\pi^2} \Lambda_{NP}^2 \lesssim (\text{TeV})^2$$

The diagram shows two loop diagrams contributing to the Higgs mass correction. The first is a top quark loop, represented by a circle with 'top' labels at the top and bottom. The second is a New Physics (NP) loop, represented by a shaded circle with 'NP' inside. Both loops are connected to external Higgs lines (dashed lines labeled 'h').

- ▶ Large **Landscape** with huge number of minima
 - Ensemble of realized vacua spans all possible EW scales
 - Anthropic selection of correct vacuum

Introduction: Solutions of the Hierarchy Problem

New solution

► “Relaxation” of the EW scale

[Graham, Kaplan, Rajendran, 1504.07551]

(see also earlier work by Abbott 85; Dvali, Vilenkin 04; Dvali 06)

- condition (i) avoided by a potential with **vacua “everywhere”**
(eg. oscillating function can have infinite set of minima)
- “correct” **minimum selected dynamically** through a backreaction of EWSB

The “minimal” realization

Higgs mass parameter \longrightarrow **Field-dependent Higgs mass**

$$m^2|H|^2$$

$$m^2(\phi)|H|^2$$

$$\text{e.g. } m^2(\phi) = \Lambda^2 \left(1 - \frac{g\phi}{\Lambda}\right)$$

- Higgs mass determined by the evolution of ϕ
- ϕ must be stabilized where $|m^2(\phi)| \ll \Lambda^2$
- this structure can arise from a “clever” dynamical interplay between H and ϕ

The “Relaxation” mechanism

The potential generate an interplay between the Higgs h and an axion-like field ϕ

$$V(\phi, h) = \Lambda^3 g \phi - \frac{1}{2} \Lambda^2 \left(1 - \frac{g\phi}{\Lambda} \right) h^2 + \varepsilon \Lambda_c^4 \left(\frac{h}{\Lambda_c} \right)^n \cos(\phi/f)$$

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“Kicking” term

makes ϕ slide forward

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ϕ “scans” the Higgs mass

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$n = 1, 2, \dots$

“self-regulating” term

stops ϕ when h turns on
(periodic function of ϕ
as for axion-like states)

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Λ cut off of the theory

Λ_c scale at which the periodic term originates

Spurions:

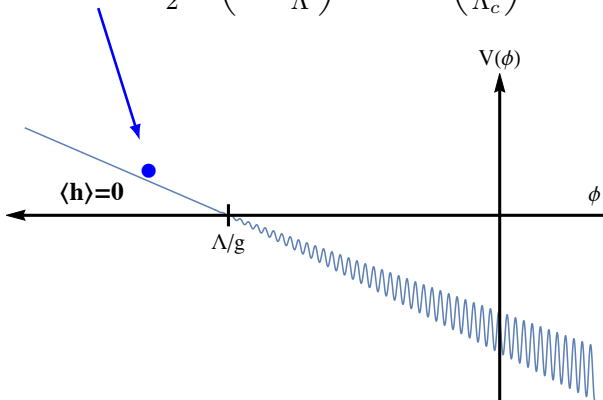
$\varepsilon \ll 1$ breaking of the shift symmetry $\phi \rightarrow \phi + c$
respecting $\phi \rightarrow 2\pi f, \phi \rightarrow -\phi$

$g \ll 1$ full breaking of the shift symmetry

The “Relaxation” mechanism

Cosmological evolution

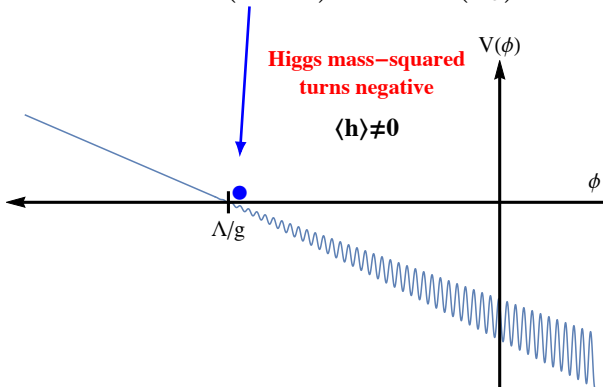
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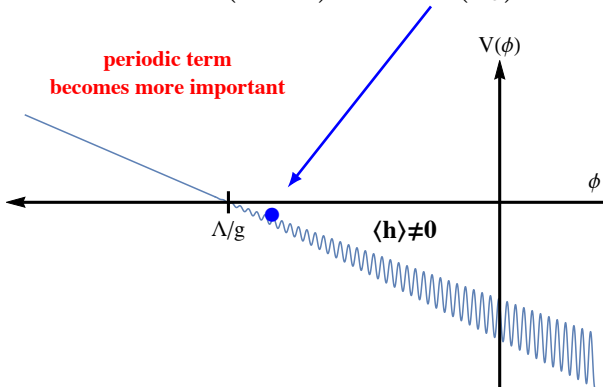
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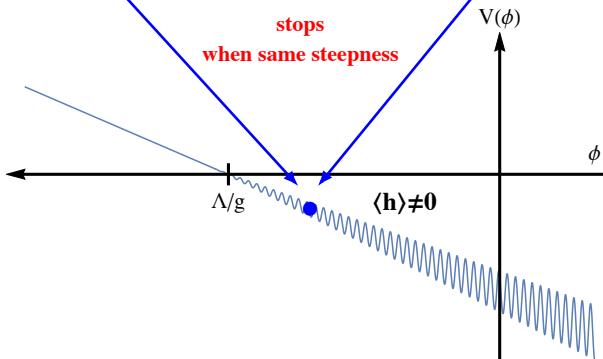
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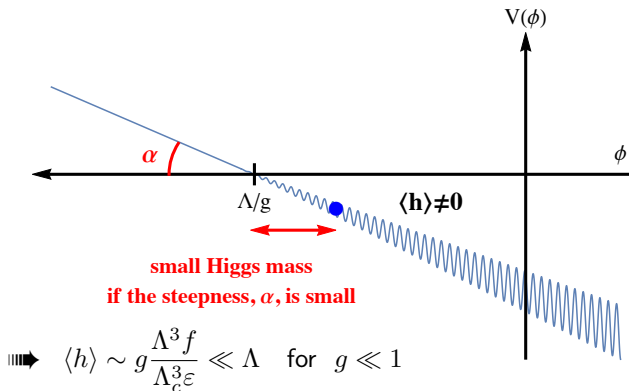
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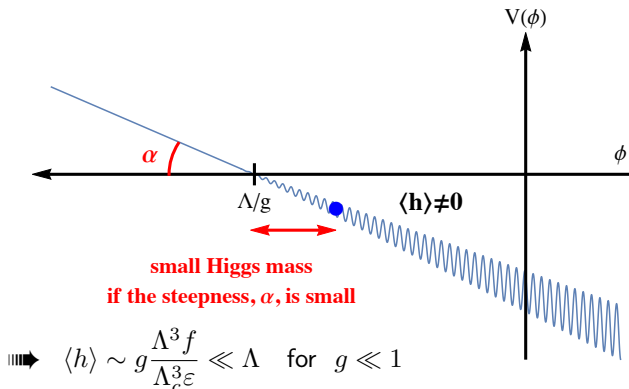
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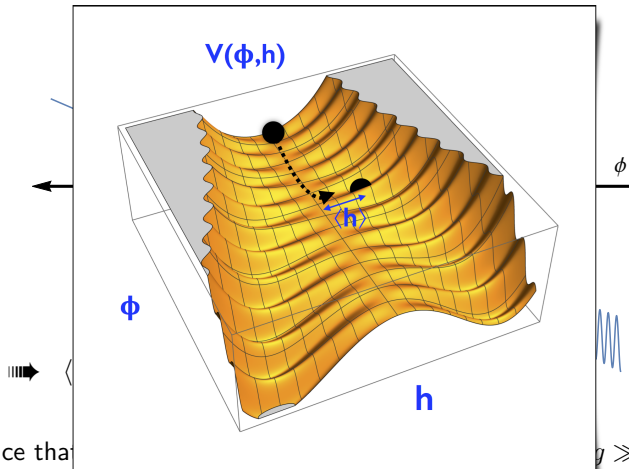


- Notice that **large field excursions** for ϕ needed: $\phi \sim \Lambda/g \gg \Lambda$

The “Relaxation” mechanism

Cosmological evolution

$$V(\phi, h) = \Lambda^3 g \phi - \frac{1}{2} \Lambda^2 \left(1 - \frac{g\phi}{\Lambda} \right) h^2 + \varepsilon \Lambda_c^4 \left(\frac{h}{\Lambda_c} \right)^n \cos(\phi/f)$$



• Notice that

$g \gg \Lambda$

The “Relaxation” mechanism

How do we stop in the correct minimum? Should we **tune the initial conditions**?

The “Relaxation” mechanism

How do we stop in the correct minimum? Should we **tune the initial conditions**?

No, if ϕ slow-rolls!

- possible if a friction is present
(eg. during the **inflationary epoch**, through Hubble friction)
- ϕ must “scan” large ranges of the Higgs mass, a long period of inflation is needed

$$\text{e-folds needed: } N_e \gtrsim \frac{H_I^2}{g^2 \Lambda^2} \sim 10^{40}$$

The “Relaxation” mechanism

Important constraint:

ϕ must slow-roll **classically** so that quantum effects do not generate a large spreading

$$\Delta\phi_{class} \sim g \frac{\Lambda^3}{H_I^2} \gtrsim \Delta\phi_{quant} \sim H_I$$



$$g \gtrsim (H_I/\Lambda)^3$$

Origin of the oscillating potential

[Graham, Kaplan, Rajendran, 1504.07551]

Which is the origin of $\varepsilon \Lambda_c^4 \left(\frac{h}{\Lambda_c} \right)^n \cos(\phi/f)$?

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axion term from **QCD condensate**: $\Lambda_c = \Lambda_{\text{QCD}}$

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problem: too large $\theta_{\text{QCD}} \sim 1$ due to linear tilt!



can be solved if the tilt disappears after inflation



Low cut-off: $\Lambda \lesssim 30 \text{ TeV}$

Which is the origin of $\varepsilon \Lambda_c^4 \left(\frac{h}{\Lambda_c} \right)^n \cos(\phi/f)$?

$n = 2$

gauge invariant, generated by new-physics at scale Λ_c
(no need to rely on QCD)

$$\varepsilon \Lambda_c^2 |H|^2 \cos(\phi/f)$$

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problem: quantum corrections from Higgs loop

$$\Rightarrow \varepsilon \Lambda_c^4 \cos(\phi/f)$$

➤ “Relaxation” only works if Higgs barrier dominates

$$\Lambda_c \lesssim v$$

New-dynamics must be around the EW scale!

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New-physics at the LHC is still required
though it arises from an “unusual” motivation
(needed to generate the periodic potential)

Extra drawback: “coincidence problem” why $\Lambda_c \sim v$?

Can we make the new-physics scale larger?

Raising the cut-off

Add an additional field σ “modulates” the periodic potential

Field-dependent amplitude

$$A \cos(\phi/f) \quad \longrightarrow \quad A(\phi, \sigma, H) = \varepsilon \Lambda^4 \left(\beta + c_\phi \frac{g\phi}{\Lambda} - c_\sigma \frac{g_\sigma \sigma}{\Lambda} + \frac{|H|^2}{\Lambda^2} \right)$$

Two “scanners” potential

$$V(\phi, \sigma, H) = \Lambda^4 \left(\frac{g\phi}{\Lambda} + \frac{g_\sigma \sigma}{\Lambda} \right) + m^2(\phi) |H|^2 + A(\phi, \sigma, H) \cos(\phi/f)$$

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spurions

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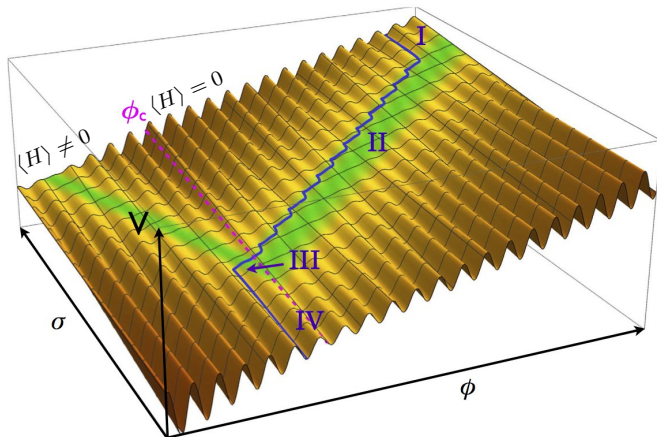
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- We take $\Lambda \sim \Lambda_c$ and see how much we can push it up

The cosmological evolution

$$V(\phi, \sigma, H) = \Lambda^4 \left(\frac{g\phi}{\Lambda} + \frac{g_{\sigma}\sigma}{\Lambda} \right) + m^2(\phi)|H|^2 + A(\phi, \sigma, H) \cos(\phi/f)$$

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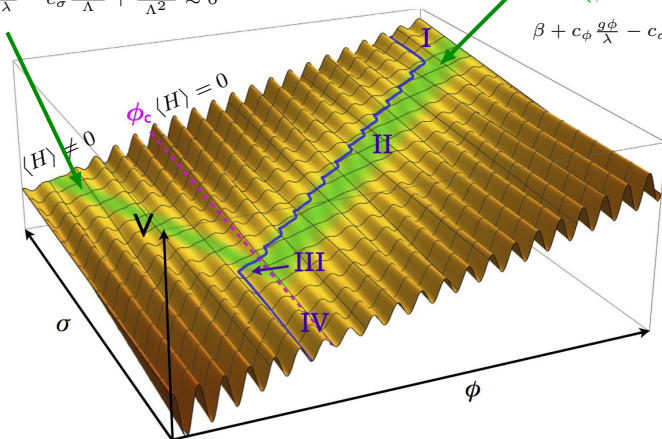
area where $A \approx 0$

$$\beta + c_{\phi} \frac{g\phi}{\Lambda} - c_{\sigma} \frac{g_{\sigma\sigma}}{\Lambda} + \frac{|H|^2}{\Lambda^2} \approx 0$$

area where $A \approx 0$

(ϕ can slow-roll)

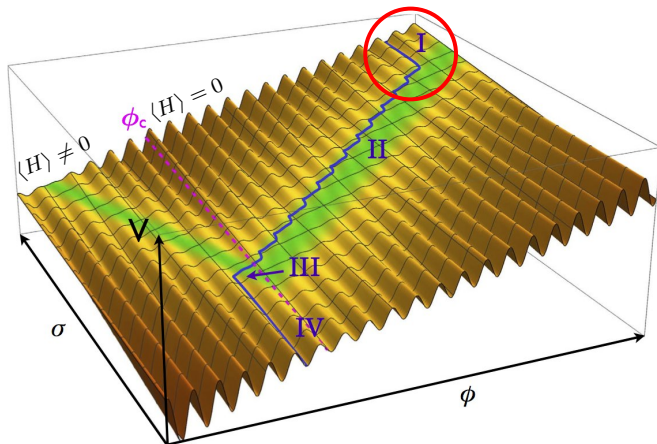
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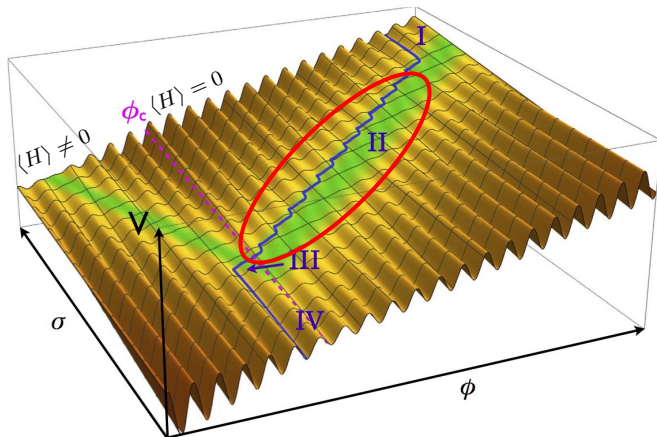


Stage I: ϕ "frozen"

The cosmological evolution

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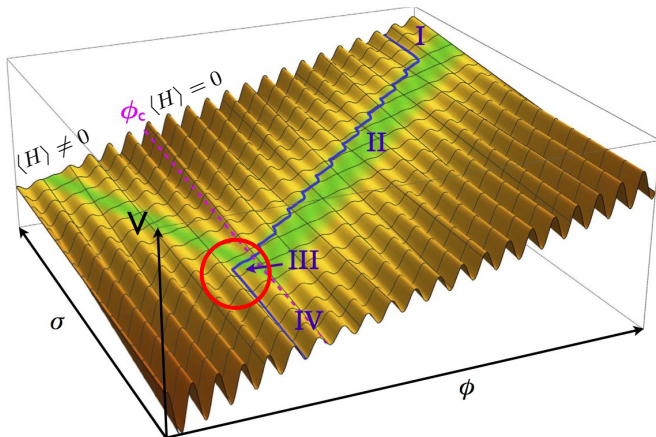


Stage II: ϕ "tracks" σ

The cosmological evolution

$$V(\phi, \sigma, H) = \Lambda^4 \left(\frac{g\phi}{\Lambda} + \frac{g_{\sigma}\sigma}{\Lambda} \right) + m^2(\phi)|H|^2 + A(\phi, \sigma, H) \cos(\phi/f)$$

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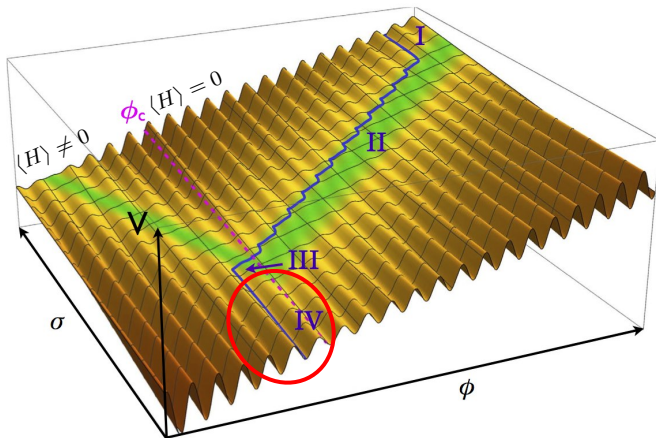


Stage III: ϕ enters the minimum

The cosmological evolution

$$V(\phi, \sigma, H) = \Lambda^4 \left(\frac{g\phi}{\Lambda} + \frac{g_{\sigma}\sigma}{\Lambda} \right) + m^2(\phi)|H|^2 + A(\phi, \sigma, H) \cos(\phi/f)$$

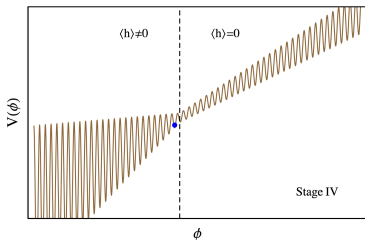
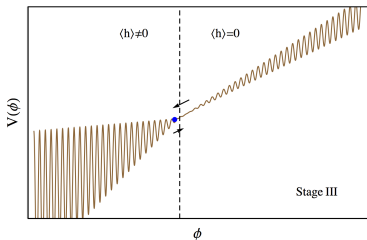
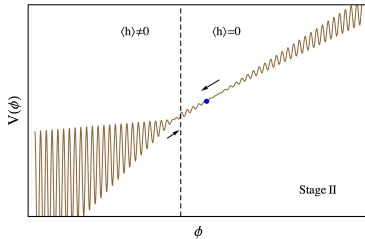
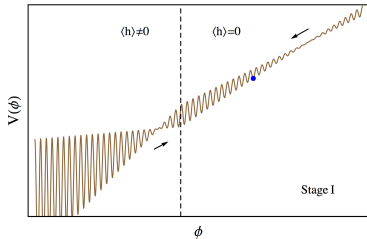
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Stage IV: ϕ stabilized

The cosmological evolution

Potential for ϕ in the four stages:



Constraints

- $\varepsilon \lesssim v^2/\Lambda^2$ keep under control quantum corrections
- $g \lesssim \Lambda/M_{Pl}$ slow-roll condition
- $H_I^3 \lesssim g_\sigma \Lambda^3$ avoid quantum effects spoiling classical rolling
- $g_\sigma \lesssim g$ allow ϕ tracking σ
- $\Lambda^2/M_{Pl} \lesssim H_I$ avoid backreaction of ϕ and σ on inflation

Stabilization of the EW scale: $v^2 \simeq \frac{g\Lambda f}{\varepsilon}$


upper bound on the cut-off

$$\Lambda \lesssim (v^4 M_{Pl}^3)^{1/7} \simeq 2 \times 10^9 \text{ GeV}$$

UV origin of the periodic term

Strong sector
a la QCD
(with light fermion, N)

+ **Axion-like ϕ**

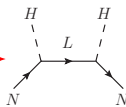

$$\frac{\phi}{f} G'_{\mu\nu} \tilde{G}'^{\mu\nu}$$

Axion potential: $V \simeq \Lambda^3 m_N \cos(\phi/f)$

Gives the needed potential if the mass of N is given by

$$m_N \simeq \varepsilon \left(\Lambda + g_\sigma \sigma + g\phi - \frac{|H|^2}{\Lambda} \right)$$

from integrating
a fermion doublet L



Phenomenological implications

- No state detectable at the LHC
- ϕ and σ are the only BSM states below Λ

light scalars weakly-coupled to the SM

$$m_\phi \sim 10^{-20} - 10^2 \text{ GeV}$$

$$m_\sigma \sim 10^{-45} - 10^{-8} \text{ GeV}$$

mixing to the SM through the Higgs:

$$|H|^2 \cos \phi / f, \quad g\phi |H|^2$$

- Benchmark values for $\Lambda \sim 10^9 \text{ GeV}$

$$m_\phi \sim 100 \text{ GeV}$$

$$\theta_{\phi h} \sim 10^{-21}$$

$$\phi\phi hh \text{ coupling} \sim 10^{-14}$$

$$m_\sigma \sim 10^{-18} \text{ GeV}$$

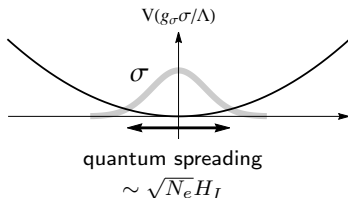
$$\theta_{\sigma h} \sim 10^{-50}$$

Cosmological consequences

➤ Many **constraints from cosmology**

dark matter overabundance, late decays, BBN bounds,
 γ -rays, CMB, pulsar timing observations, ...

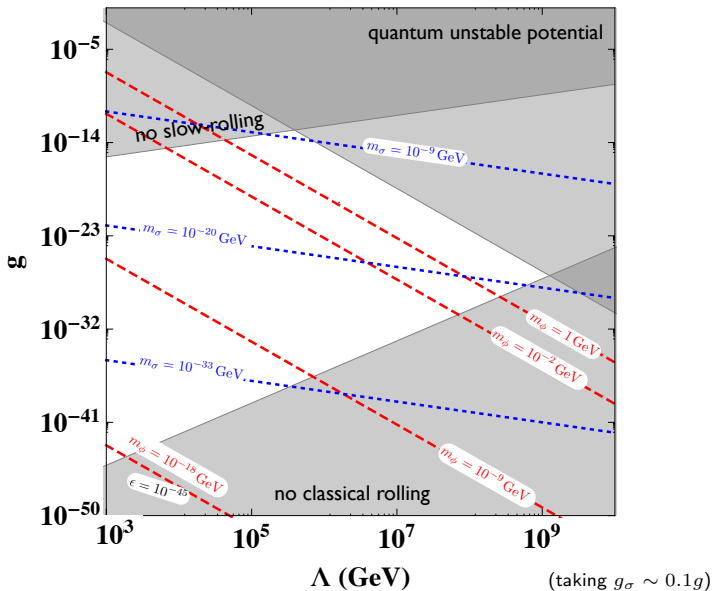
➤ Oscillations of σ can provide a **Dark Matter candidate**



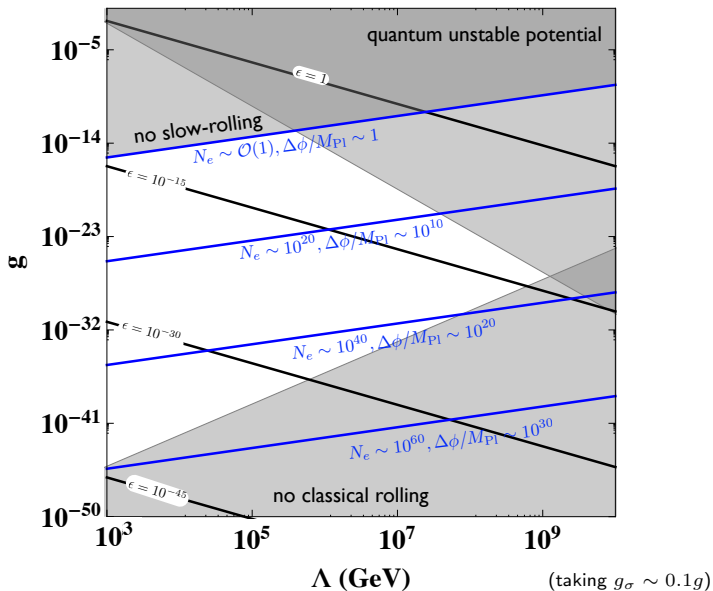
$$\Rightarrow \rho_{ini}^\sigma \sim H_I^4$$

$$\rho_\sigma(T) \sim \rho_{ini}^\sigma (T/T_{osc})^3 \Rightarrow \Omega_\sigma \gtrsim \left(\frac{10^{-27}}{g_\sigma}\right)^{3/2} \left(\frac{\Lambda}{10^8 \text{ GeV}}\right)^{13/2}$$

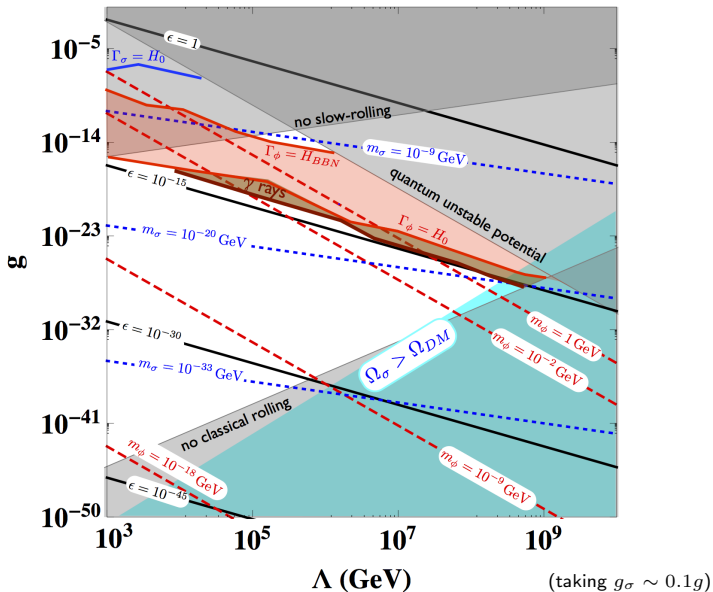
Parameter space



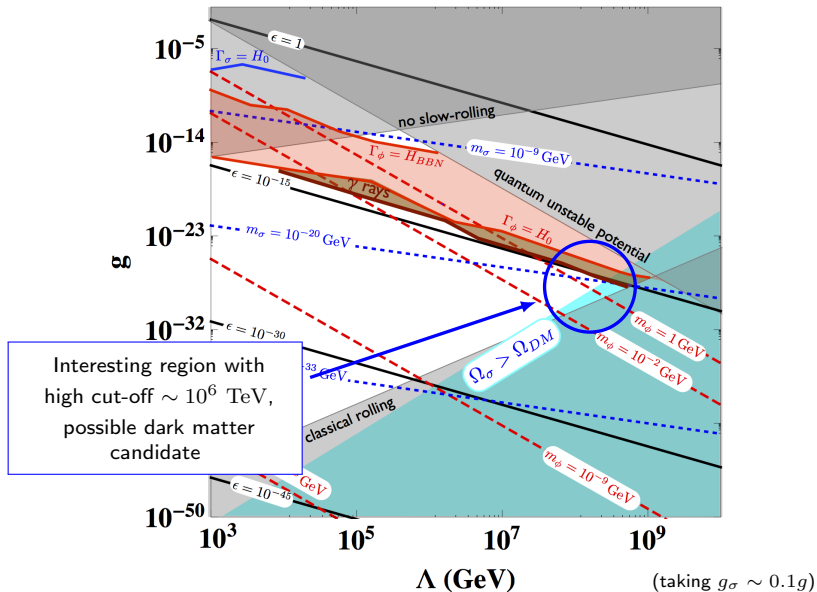
Parameter space



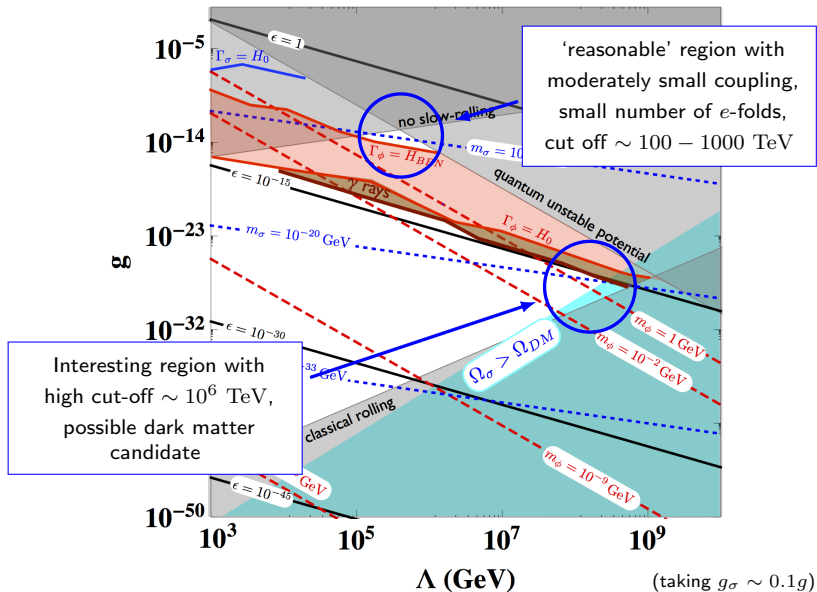
Constraints on the parameter space



Constraints on the parameter space



Constraints on the parameter space



Conclusions

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The “**Relaxation**” **models** provide an “existence proof” of **natural theories** with a high cut-off scale ($\Lambda \sim 10^9$ GeV)

Good features:

Change of paradigm

- new physics is given by weakly-coupled light states
- not detectable at high-energy collider experiments

Other type of experiments needed

- astrophysics (γ -rays, pulsar timing, ...), CMB, fifth-force searches, ...

Ugly features:

Huge number of inflation e-folds $N_e > 10^{38}$ (if high cut-off is required)

Super-Planckian field excursions

Future directions:

- ▶ Are there ways to avoid the limit on the cut-off $\Lambda \lesssim 10^9$ GeV?
- ▶ UV completion? How to get the double breaking of the shift symmetry in the “axion” potential? Connection with SUSY?

[see Gupta, Komargodski, Perez and Ubaldi, arXiv:1509.00047,
Batell, Giudice, McCullough, arXiv:1509.00834]

- ▶ Find suitable inflationary models with huge N_e
- ▶ Alternative sources of friction, disentangling the “relaxation” mechanism from inflation
 - proposal to do this at finite temperature [Hardy, arXiv:1507.07525]